

# PHYS 212, Honors Section, Spring 2011 – Review Material

Part 2/2, Chapters 29-40

## Chapter 29: Magnetic Fields

- Magnetic force: On a moving charge  $\mathbf{F} = q \mathbf{v} \times \mathbf{B}$ , on a current  $\mathbf{F} = I \mathbf{L} \times \mathbf{B}$ , or  $F = ILB \sin\theta$ .
- Path of a particle: In a constant magnetic field, a particle moves on a circle with  $r = mv/qB$ .
- Torque on a current loop: The magnetic dipole moment and torque on the loop are  $\boldsymbol{\tau} = \boldsymbol{\mu} \times \mathbf{B}$ ,  $\boldsymbol{\mu} = NIA \hat{n}$ .

## Chapter 30: Sources of the Magnetic Field

- Biot-Savart law: For a wire element  $d\mathbf{s}$ ,  $d\mathbf{B} = (\mu_0/4\pi) (I d\mathbf{s} \times \mathbf{r})/r^2$ , where  $\mu_0 = 4\pi \times 10^{-7} \text{ T}\cdot\text{m/A}$ .
- Examples: For a long straight wire,  $B = (\mu_0/2\pi) I/r$ ; For a circular wire  $B = (\mu_0/4\pi) I \phi/r$ .
- Magnetic force between wires carrying currents: For two long straight wires  $F = (\mu_0/2\pi) (I_1 I_2/a) L$ .
- Ampère's law: For any closed loop  $C$  in space enclosing a current  $I_{\text{enc}}$ ,  $\int_C \mathbf{B} \cdot d\mathbf{s} = \mu_0 I_{\text{enc}}$ .
- Magnetic field of a long solenoid: The magnitude of the field is  $B = \mu_0 nI$  ( $n = N/L$ ).

## Chapter 31: Faraday's Law

- Magnetic flux: The flux of  $\mathbf{B}$  through a surface  $S$  is  $\Phi_B = \int_S \mathbf{B} \cdot d\mathbf{A}$ .
- Faraday's law: When  $\Phi_B$  changes in time,  $\mathcal{E} = -N d\Phi_B/dt$ , or  $\int_C \mathbf{E} \cdot d\mathbf{s} = -d\Phi_B/dt$ .
- Motional emf: The potential difference induced across a moving conductor,  $\mathcal{E} = \hat{v} \cdot \mathbf{B} l$ .

## Chapter 34: Electromagnetic Waves

- Maxwell's equations: They contain all information on how electric and magnetic fields are produced,

$$\int_S \mathbf{E} \cdot d\mathbf{A} = q_{\text{enc}}/\epsilon_0, \int_C \mathbf{E} \cdot d\mathbf{s} = -d\Phi_B/dt, \int_S \mathbf{B} \cdot d\mathbf{A} = 0, \int_C \mathbf{B} \cdot d\mathbf{s} = \mu_0 I_{\text{enc}} + \mu_0 \epsilon_0 d\Phi_E/dt.$$

- Electromagnetic waves: Plane harmonic waves  $E = E_{\text{max}} \cos(kx - \omega t)$  and  $B = B_{\text{max}} \cos(kx - \omega t)$ , with  $k = 2\pi/\lambda$ ,  $\omega = 2\pi f$  and, as for all waves,  $\lambda f = v$ , the speed;  $E/B = c$ ,  $c = (\mu_0 \epsilon_0)^{-1/2} = 3.00 \times 10^8 \text{ m/s}$ .
- Energy, momentum: Poynting vector  $\mathbf{S} = (1/\mu_0) \mathbf{E} \times \mathbf{B}$ ,  $P = S/c$  or  $2S/c$  (absorbing or reflecting surface).

## Chapter 35, 36: The Nature of Light and Ray Optics, and Image Formation

- Reflection: The law of reflection,  $\theta_1' = \theta_1$ .
- Refraction: Index of refraction  $n = c/v$ ; The law of refraction,  $n_1 \sin \theta_1 = n_2 \sin \theta_2$ .
- Curved mirrors: Focal length  $f = R/2$ ; Mirror equation  $1/p + 1/q = 1/f$ ; and  $M = h'/h = -q/p$ .

## Chapters 37, 38: Wave Optics and Diffraction Patterns and Polarization

- Interference pattern: For two thin slits, bright fringes are located at  $d \sin \theta = m\lambda$ , with  $m = 0, \pm 1, \pm 2, \dots$
- Diffraction pattern: For a narrow slit, dark fringes are located at  $a \sin \theta = m\lambda$ , with  $m = \pm 1, \pm 2, \dots$

## Chapters 39, 40: Relativity and Introduction to Quantum Physics

- Length contraction, time dilation:  $L = L_p / \gamma$ , and  $\Delta t = \gamma \Delta t_p$ ,  $\gamma = 1/(1-v^2/c^2)^{1/2}$ .
- Light as particles:  $E = hf$ , where  $h = 6.63 \times 10^{-34} \text{ J}\cdot\text{s}$  is Planck's constant; Wavelength  $\lambda = h/p$ .
- Uncertainty principle:  $\Delta x \Delta p \geq (1/2) h/2\pi$ .