

Increment of Energy stored in capacitor:

$$dU_E = V(q')dq'$$

$$U_E = \int_0^q V(q')dq' = \int_0^q \frac{q'}{C}dq' = \frac{1}{2} \frac{q^2}{C} = \frac{1}{2} CV^2$$

