

BETA DECAY SPECTROMETER

Purpose:

We will measure electron energy spectrum for two radioactive beta emitters, Sr90 and Tl204. The average Q and endpoint energy will be observed. The spectrum is not monochromatic, but is characteristic of a 3-body decay where the beta may take on a spectrum of energies.

$P \rightarrow D + e^- + \nu$ Parent \rightarrow Daughter + beta- + neutrino

The Q -value of the decay is the total kinetic energy available to the decay products.

$$Q = M(P) - M(D) - M(e) - M(\nu)$$

Q is shared equally amongst the three decay products, so

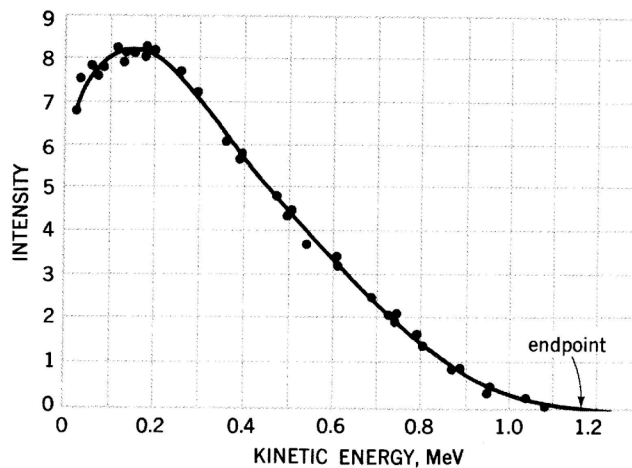
$$\langle Q \rangle \sim Q/3$$

The maximum T_{\max} a decay product may receive is Q !

$$T_{\max} = Q \text{ (endpoint)}$$

Thus by measuring the electron's kinetic energy spectrum of we can determine $T_{\max} = Q$.

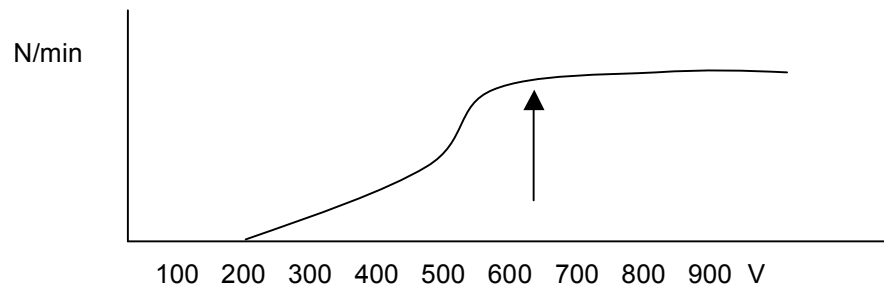
FIGURE 11-1 Energy spectrum of electrons emitted in the beta decay of Bi^{210} . [From G. J. Neary, *Proc. Phys. Soc. (London)*, **A175**: 71 (1940).]



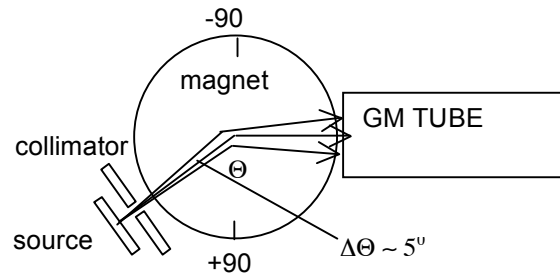
(1) HV Plateau Before using the beta spectrometer with the GM tube you should find the GM tube operating voltage by moving the source to the zero $+70^\circ$ position and record the number of counts per 10-minute interval, each 100V between 300 V and 800V.

Graph the result and identify the plateau region. The Geiger tube voltage should be set to a value about 20% past the onset of the plateau.

V	100	200	300	400	500	600	700	800	900
N/min									



(2) Take counts per 10 minute interval each 10 degrees (0 to + 90 degrees.).



Angle	0	10	20	30	40	50	60	70	80	90
Counts/10m										

(3) Graph the number of counts above background per energy interval versus electron kinetic energy. dN/dE vs T .

$$\frac{dN}{dT} = \left(\frac{dN}{d\theta} \right) \left(\frac{d\theta}{dT} \right) \quad \text{with} \quad \left(\frac{d\theta}{dT} \right) \sim \left(\frac{\Delta\theta}{\Delta T} \right) = \left| \frac{5^\circ}{T(\theta + 2.5^\circ) - T(\theta - 2.5^\circ)} \right| \quad (\text{See BetaCalculator.xls on web site.})$$

Determine the endpoint energy Q where the energy spectrum merges in to the background.

Derivation of Kinetic Energy Equation

$$T = E - mc^2 \quad \text{and} \quad p = qBr = eBR / \tan(\theta/2)$$

$$T = \sqrt{p^2 c^2 + m^2 c^4} - mc^2 = mc^2 \left[\sqrt{\left(\frac{pc}{mc^2} \right)^2 + 1} - 1 \right] = mc^2 \left[\sqrt{\left(\frac{eBR}{mc \tan(\theta/2)} \right)^2 + 1} - 1 \right]$$

$$\text{with} \quad \left(\frac{eBR}{mc} \right) = 1.131$$

$$T = 0.511 \left[\sqrt{\left(\frac{1.131}{\tan(\theta/2)} \right)^2 + 1} - 1 \right] \text{ MeV}$$

