

CHAPTER 13 HOMEWORK

#4- (a) $hf = 2 \mu_B = 2 g_n \mu_B = 2 (1.9135)(5.05 \times 10^{-27} \text{ J/T})(1\text{T}) = 1.93 \times 10^{-26} \text{ J}$
 $f_n = 1.93 \times 10^{-26} \text{ J} / h = 1.93 \times 10^{-26} \text{ J} / 6.63 \times 10^{-34} \text{ J-s} = \underline{29.1 \text{ Mhz}}$

(b) $hf = 2 \mu_B = 2 g_p \mu_B = 2 (2.7928)(5.05 \times 10^{-27} \text{ J/T})(1\text{T}) = 1.93 \times 10^{-26} \text{ J}$
 $f_p = 2.82 \times 10^{-26} \text{ J} / h = 2.82 \times 10^{-26} \text{ J} / 6.63 \times 10^{-34} \text{ J-s} = \underline{42.5 \text{ MHz}}$

(c) $f = 2 \mu_B / h = 2 (2.7928)(5.05 \times 10^{-27} \text{ J/T})(50 \times 10^{-6} \text{ T}) / h = \underline{2.13 \text{ kHz}}$

#5- $KE_\alpha = 0.5 \text{ MeV}$ $z_1 = 2$ $Z_2 = 79$

(a) $KE_\alpha = k q_1 q_2 / R = k z_1 Z_2 e^2$
 $R = k q_1 q_2 / KE = (9 \times 10^9 \text{ Nm}^2/\text{C}) (2)(79) e^2 / (500 \times 10^3 \text{ e V})$
 $R = (9 \times 10^9 \text{ Nm}^2/\text{C}) (2)(79) (1.6 \times 10^{-19} \text{ C}) / (500 \times 10^3 \text{ V}) = 4.55 \times 10^{-13} \text{ m}$
 $\underline{R \leq 455 \text{ fm}}$ The nuclear radius must at least this small!

(b) $v = \sqrt{2KE/m} = \underline{6.0 \times 10^6 \text{ m/s}}$

#15- $BE_X = Z M_p + N M_n - M(X)$

(a) $^{20}\text{Ne}_{10}$
 $BE = [10(1.007825\text{u}) + 10(1.008665\text{u}) - (19.992436\text{u})]931.494 \text{ MeV/u}$
 $BE = 160.650 \text{ MeV}$ $\underline{BE/A = 8.04 \text{ MeV/nucleon}}$

(b) $^{40}\text{Ca}_{20}$
 $BE = [20(1.007825\text{u}) + 20(1.008665\text{u}) - (39.962591)]931.494 \text{ MeV/u}$
 $BE = 342.053 \text{ MeV}$ $\underline{BE/A = 8.55 \text{ MeV/nucleon}}$

(c) $^{93}\text{Nb}_{41}$
 $BE = [41(1.007825\text{u}) + 52(1.008665\text{u}) - (92.906377)]931.494 \text{ MeV/u}$
 $BE = 805.768 \text{ MeV}$ $\underline{BE/A = 8.66 \text{ MeV/nucleon}}$

(d) $^{197}\text{Au}_{79}$
 $BE = [79(1.007825\text{u}) + 118(1.008665\text{u}) - (196.996543)]931.494 \text{ MeV/u}$
 $BE = 1559.416 \text{ MeV}$ $\underline{BE/A = 7.92 \text{ MeV/nucleon}}$

#23- (a) From $R = R_0 e^{-\lambda t}$
 $\lambda = 1/t \ln\{R_0/R\} = 1/4\text{h} \ln(10/8) = 5.58 \times 10^{-2} \text{ hr}^{-1} = \underline{1.55 \times 10^{-5} \text{ s}^{-1}}$
 $T_{1/2} = 0.693/\lambda = \underline{12.4 \text{ h}}$

(b) $R_0 = 10 \text{ mCi} = 10 \times 10^{-3} \text{ } 3.7 \times 10^{10} \text{ decays/s} = 3.7 \times 10^8 \text{ 1/s}$
 $N_0 = R_0/\lambda = 3.7 \times 10^8 \text{ s}^{-1} / 1.55 \times 10^{-5} \text{ s}^{-1} = \underline{2.39 \times 10^{13} \text{ atoms}}$

(c) $R = R_0 e^{-\lambda t} = (10 \text{ mCi}) \exp\{-(5.58 \times 10^{-2} \text{ hr}^{-1})(30 \text{ hr})\} = \underline{1.87 \text{ mCi}}$

#38 - $R = 10 \text{ Ci}$ at $t=30 \text{ mo.} = 2.5 \text{ y}$ Co^{60}
 $\lambda = 0.692/5.2 \text{ y} = 0.133 \text{ y}^{-1} = 4.22 \times 10^{-9} \text{ s}^{-1}$
Using $R = R_0 e^{-\lambda t}$ $R_0 = N_0 \lambda$

(a) $10 \text{ Ci} = N_0 \lambda e^{-2.5 \text{ y} \lambda}$
 $N_0 = (10 \text{ Ci} / \lambda) e^{2.5 \text{ y} \lambda}$
 $= [(3.7 \times 10^{11} \text{ decays/s}) / 4.22 \times 10^{-9} \text{ s}^{-1}] \exp\{(2.5 \text{ y})(0.133 \text{ y}^{-1})\}$
 $= 1.22 \times 10^{20} \text{ atoms}$
 $m = (N_0/N_A) 60 \text{ g/mole} = 1.22 \times 10^{-2} \text{ g} = \mathbf{12.2 \text{ mg}}$

(b) $R(t=2.5 \text{ y}) = 10 \text{ Ci} = 3.7 \times 10^{11} \text{ decays/s}$ *Activity at $t=2.5 \text{ y}$*

$Power = dE/dt = E dN/dt = E R$
 $= \{0.31 + 1.17 + 1.33\} \text{ MeV/decay} \times 3.7 \times 10^{11} \text{ decays/s}$
 $= 1.04 \times 10^{12} \text{ MeV/s} = 0.166 \text{ J/s} = \mathbf{166 \text{ mW}}$

#41- $Q = M(^{238}\text{U}) - M(^{234}\text{Th}) - M(^4\text{He}) \times 931.5 \text{ MeV/u}$
 $Q = 238.048608 \text{ u} - 234.043583 \text{ u} - 4.002603 \text{ u} \times 931.5 \text{ MeV/u} = \mathbf{2.26 \text{ MeV OR}}$
 $Q = 238.050785 \text{ u} - 234.043593 \text{ u} - 4.002603 \text{ u} \times 931.5 \text{ MeV/u} = \mathbf{4.27 \text{ MeV}}$

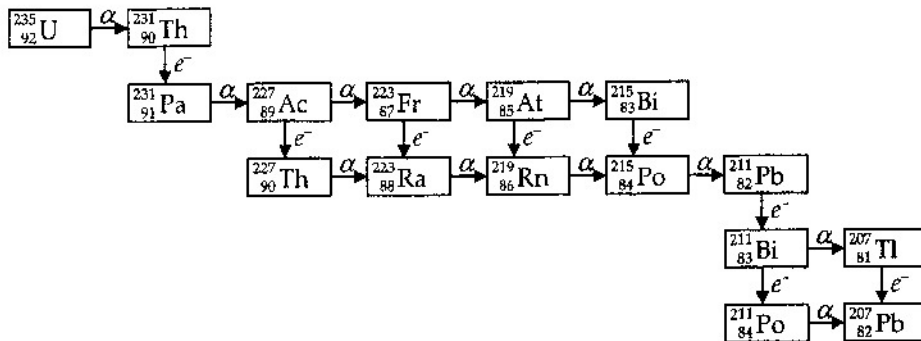
#45- $Q = M(X^{\text{Initial}}) - M(X^{\text{Final}}) \times 931.5 \text{ MeV/u}$

(a) $Q = \{M(^{40}\text{Ca}_{20}) - M(^{40}\text{Ca}_{19}) - M(^0\text{e}_1)\} \times 931.5 \text{ MeV/u}$
 $Q = \{39.96259 \text{ u} - 0.000548 \text{ u} - 39.964 \text{ u}\} \times 931.5 \text{ MeV/u}$
 $Q = \mathbf{-1.82 \text{ MeV}}$ *will not occur unless energy supplied*

(b) $Q = \{M(^{98}\text{Ru}_{44}) - M(^4\text{He}_2) - M(^{94}\text{Mo}_{42})\} \times 931.5 \text{ MeV/u}$
 $Q = \{97.9055 \text{ u} - 4.0026 \text{ u} - 93.9077 \text{ u}\} \times 931.5 \text{ MeV/u}$
 $Q = \mathbf{-1.68 \text{ MeV}}$ *will not occur unless energy supplied*

(c) $Q = \{M(^{144}\text{Nd}_{60}) - M(^4\text{He}_2) - M(^{140}\text{Ce}_{58})\} \times 931.5 \text{ MeV/u}$
 $Q = \{143.9099 \text{ u} - 4.0026 \text{ u} - 139.9054 \text{ u}\} \times 931.5 \text{ MeV/u}$
 $Q = \mathbf{-1.86 \text{ MeV}}$ *can occur spontaneously*

#50-



#59- $R = (0.12 \pm 0.01) \text{ Bq per gram of Carbon}$

$T_{1/2} = 5730 \text{ y}$

$$\lambda = 0.693 / T_{1/2} = 1.21 \times 10^{-4} \text{ y}^{-1}$$

$$\text{and } N_0 = (1/12) N_A = 5.02 \times 10^{22} \text{ atoms}$$

$$R_0 = N_0 \lambda = 0.25 \text{ Bq}$$

Original Activity C14 in the atmosphere

$$R = 0.12 \text{ Bq}$$

Current Activity

$$\text{Using } R = R_0 e^{-\lambda t}$$

$$t (R=0.12 \text{ Bq}) = -\ln(R/R_0)/\lambda = -\ln(0.12/0.25)/(1.21 \times 10^{-4} \text{ y}^{-1}) = 6066 \text{ y}$$

$$t (R=0.11 \text{ Bq}) = -\ln(R/R_0)/\lambda = -\ln(0.11/0.25)/(1.21 \times 10^{-4} \text{ y}^{-1}) = 6785 \text{ y}$$

$$t (R=0.13 \text{ Bq}) = -\ln(R/R_0)/\lambda = -\ln(0.13/0.25)/(1.21 \times 10^{-4} \text{ y}^{-1}) = 5404 \text{ y}$$

$$t \sim (6066 \pm 690) \text{ y}$$