Student name: _____

5-minute Quiz #9

Answer these two questions:

1. In a pairs skating competition a male 80-kg skater is carrying his 40-kg partner. The couple is gliding backward at a constant speed of -3 m/s with respect to the rink. What is the momentum of the couple with respect to the rink? *[2 points]* What is the speed of the male skater after he throws his partner forward at a speed 1.50 m/s relative to the ice? *[3 points]*

2. A 500-kg cannon fires a 20-kg cannon ball at a speed of 400 m/s. The explosion lasts 1 ms. What is the recoil speed of the cannon? *[3 points]*. What is the average force applied by the ball on the cannon? *[2 points]*

Key Equations

Definition of momentum	$\vec{\mathbf{p}} = m\vec{\mathbf{v}}$
Impulse	$\vec{J} \equiv \int_{t_i}^{t_f} \vec{F}(t)dt \text{ or } \vec{\mathbf{J}} = \vec{\mathbf{F}}_{\text{ave}}\Delta t$
Impulse-momentum theorem	$\vec{\mathbf{J}} = \Delta\vec{\mathbf{p}}$
Average force from momentum	$\vec{\mathbf{F}} = \frac{\Delta\vec{\mathbf{p}}}{\Delta t}$
Instantaneous force from momentum (Newton's second law)	$\vec{\mathbf{F}}(t) = \frac{d\vec{\mathbf{p}}}{dt}$
Conservation of momentum	$\frac{d\vec{\mathbf{p}}_1}{dt} + \frac{d\vec{\mathbf{p}}_2}{dt} = 0 \text{ or } \vec{\mathbf{p}}_1 + \vec{\mathbf{p}}_2 = \text{constant}$
Generalized conservation of momentum	$\sum_{j=1}^{N} \vec{\mathbf{p}}_\mathbf{j} = \text{constant}$
Conservation of momentum in two dimensions	$p_{\text{f},x} = p_{1,\text{i},x} + p_{2,\text{i},x}$ $p_{\text{f},y} = p_{1,\text{i},y} + p_{2,\text{i},y}$
External forces	$\vec{\mathbf{F}}_{\text{ext}} = \sum_{j=1}^{N} \frac{d\vec{\mathbf{p}}_j}{dt}$
Newton's second law for an extended object	$\vec{\mathbf{F}} = \frac{d\vec{\mathbf{p}}_{\text{CM}}}{dt}$
Acceleration of the center of mass	$\vec{\mathbf{a}}_{\text{CM}} = \frac{d^2}{dt^2}\left(\frac{1}{M}\sum_{j=1}^{N} m_j\vec{\mathbf{r}}_j\right) = \frac{1}{M}\sum_{j=1}^{N} m_j\vec{\mathbf{a}}_j$
Position of the center of mass for a system of particles	$\vec{\mathbf{r}}_{\text{CM}} \equiv \frac{1}{M}\sum_{j=1}^{N} m_j\vec{\mathbf{r}}_j$
Velocity of the center of mass	$\vec{\mathbf{v}}_{\text{CM}} = \frac{d}{dt}\left(\frac{1}{M}\sum_{j=1}^{N} m_j\vec{\mathbf{r}}_j\right) = \frac{1}{M}\sum_{j=1}^{N} m_j\vec{\mathbf{v}}_j$
Position of the center of mass of a continuous object	$\vec{\mathbf{r}}_{\text{CM}} \equiv \frac{1}{M}\int \vec{\mathbf{r}}\, dm$