

# Future Tests of General Relativity with Gravitational Waves

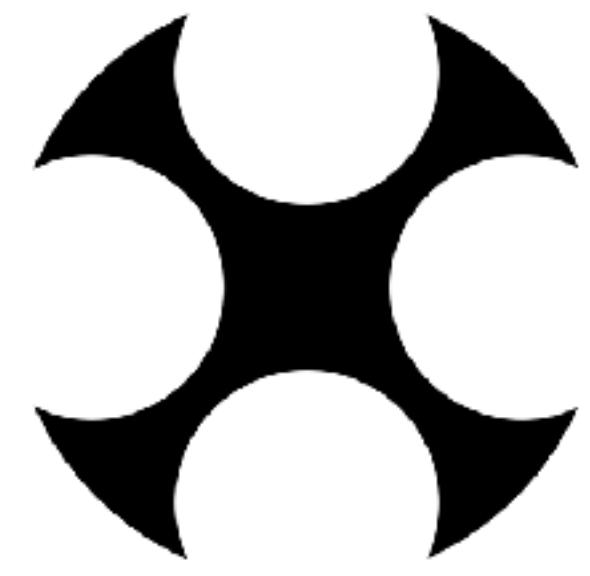
Nicolas Yunes  
eXtreme Gravity Institute  
Montana State University

StronG BaD Workshop  
March 2nd, 2017

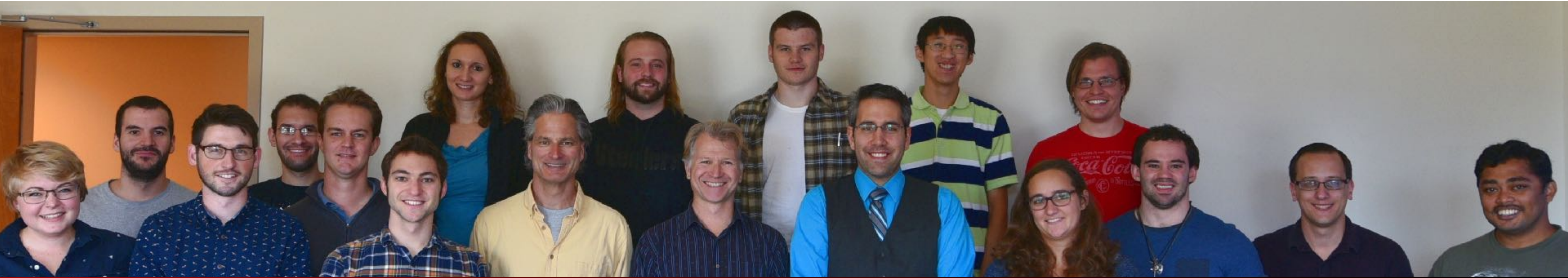
Barausse, Yunes, Chamberlain, arXiv 1603.04075, PRL (2016)  
Yunes, Yagi, Pretorius, arXiv 1608.06187, PRD (2016)  
Chamberlain and Yunes, to be submitted (very soon!)



# eXtreme Gravity Institute



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Contact: [ncornish@montana.edu](mailto:ncornish@montana.edu)

Date: 2017-08-17 - 2017-08-19

Location: Bozeman, Montana, USA

## eXtreme Matter meets eXtreme Gravity Workshop, Bozeman, Montana, USA

XGI Workshop First Announcement:

"eXtreme Matter meets eXtreme Gravity"

August 17-19, Bozeman Montana

The eXtreme Gravity Institute at Montana State University will hold a workshop to discuss methods for constraining the properties of Neutron Stars and the dense-matter equation of state. Like previous XGI workshops, the format will emphasize discussion and exchange of ideas over formal presentations. Each session will be organized around a science question, with a moderator and two discussion leaders. Topics to be covered include gravitational-wave observations of Neutron Star – Neutron Star and Neutron Star – Black Hole binaries, X-ray observations by the NICER mission (set to launch very soon), theoretical calculations of the dense-matter equation of state, and numerical simulations of NS-NS and NS-BH mergers.

The meeting is being held immediately prior to the HEAD meeting in Sun Valley, and participants may choose to drive between the meetings, or simply head a little south of Bozeman to view the total eclipse on the 21st of August. Bozeman is a beautiful mountain town a one-hour drive from the North entrance of Yellowstone National Park. The surrounding area offers great opportunities for hiking, fishing, white water rafting, and mountain biking.

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#### CONFERENCES

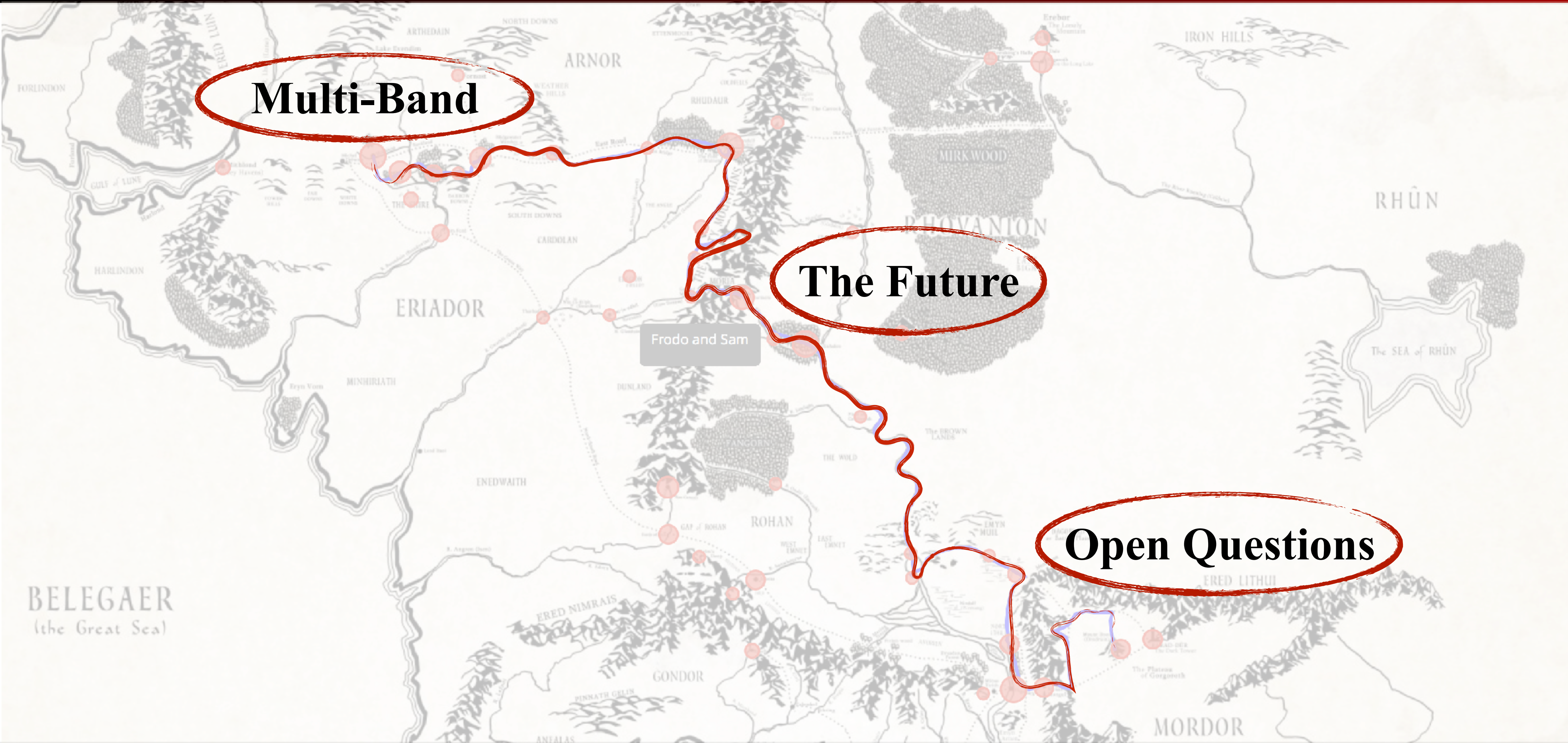
- [ICRANet-Minsk workshop on high energy astrophysics, Minsk, Belarus](#)
- [Fifth Galileo-Xu Guangqi Meeting, Chengdu, China](#)
- [15th Italian-Korean Symposium on Relativistic Astrophysics, Seoul, Korea](#)
- [Geometric Foundations of Gravity in Tartu, Estonia](#)
- [3rd Karl Schwarzschild Meeting – Gravity and the Gauge/Gravity Correspondence, Frankfurt, Germany](#)

#### JOBBS

- [Assistant Lecturer in Gravitational Wave Astrophysics at Monash University, Australia](#)
- [Professor/Reader in Gravitational Wave Science at Portsmouth, UK](#)



# Roadmap



**Multi-Band**

**The Future**

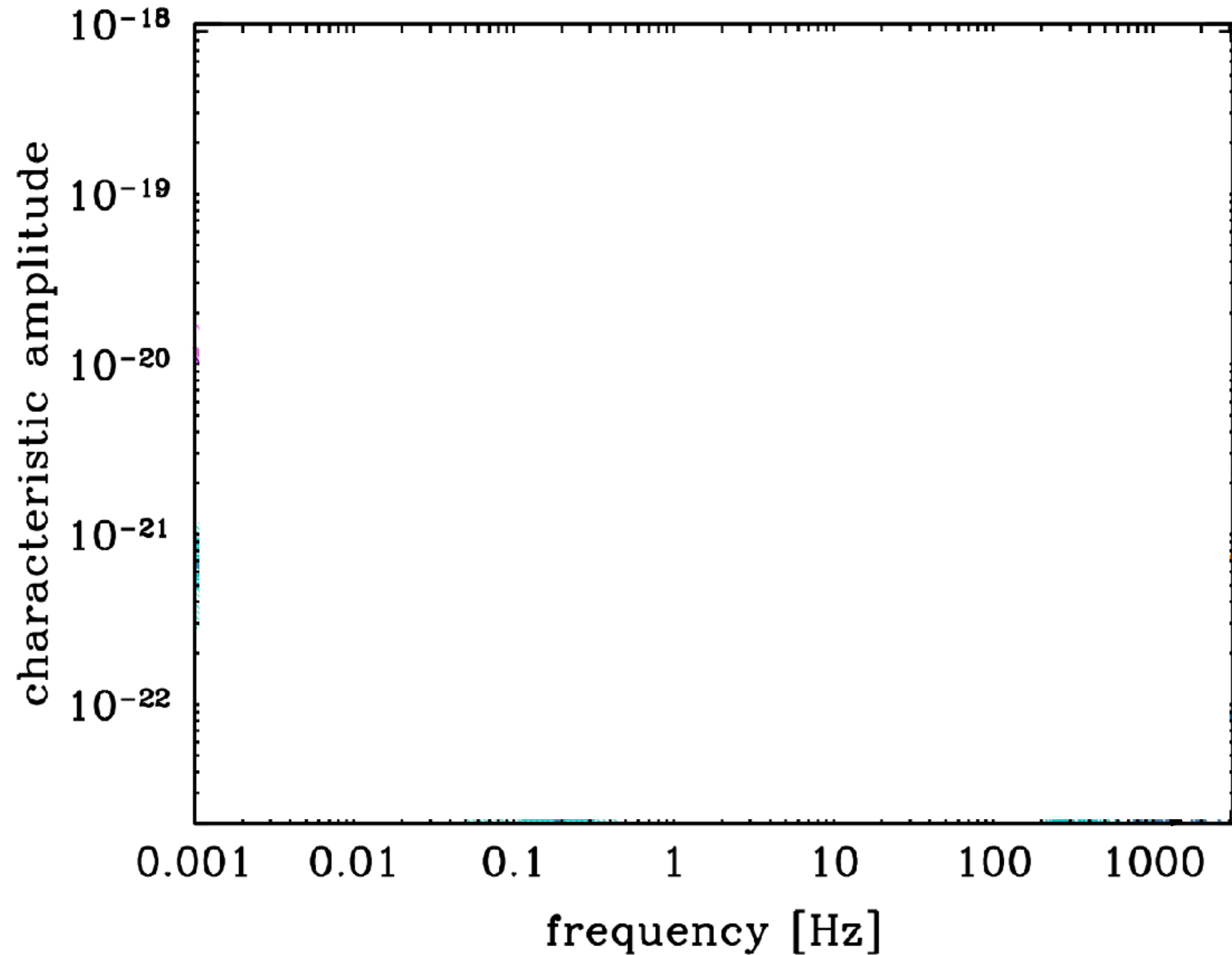
**Open Questions**

Frodo and Sam

BELEGAER  
(the Great Sea)



# Multi-Band Observations



[Amaro-Seoane &  
Santamaria Ap.J. '10,  
Sesana, PRL '16]







## Faster Inspiral, Faster Merger

$$\frac{df_{\text{GW}}}{dt} = \left( \frac{df_{\text{GW}}}{dE_b} \right) \left( \frac{dE_b}{dt} \right) = - \left( \frac{df_{\text{GW}}}{dE_b} \right) \dot{E}_{\text{GW}} = - \left( \frac{df_{\text{GW}}}{dE_b} \right) \left[ \left( \frac{m}{r_{12}} \right)^5 + B \left( \frac{m}{r_{12}} \right)^4 \right]$$

## Faster Inspiral, Faster Gravitational Wave Chirp

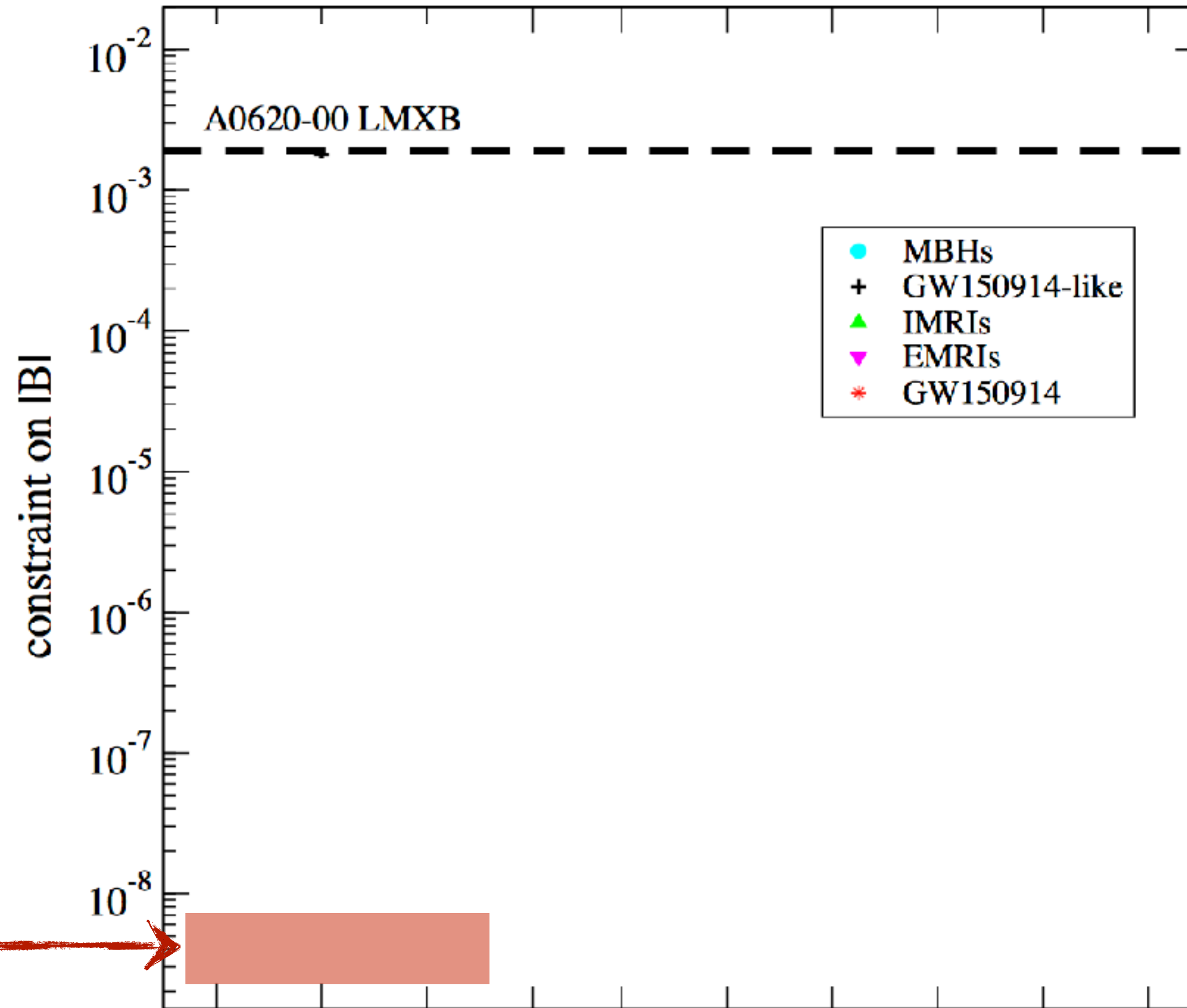
$$\Psi_{\text{GW}} \propto \int^t \int^{t'} \left( \frac{df_{\text{GW}}}{dt''} \right) dt'' dt' = \Psi_{\text{GW,GR}} + \beta(B) (\pi \mathcal{M} f_{\text{GW}})^{-7/3}$$

↑  
Quadrupole +  
Octopole + ...

↑  
Dipole  
GW Term



# Projected Constraints on Dipole Radiation



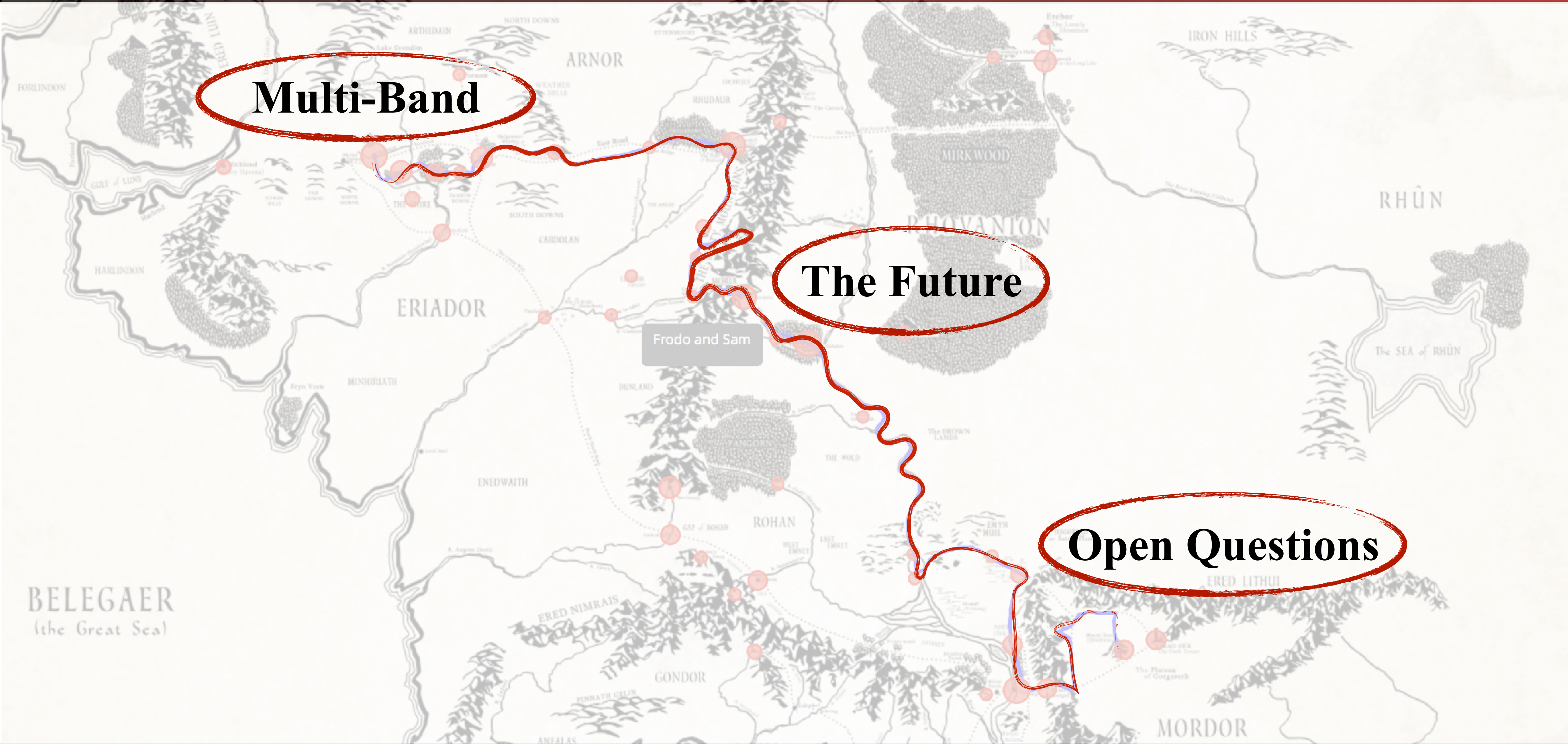
**10<sup>6</sup> times better than current bounds!!**

$$\beta = -\frac{3}{224}\eta^{2/5}B$$

[Barausse, Yunes, Chamberlain, PRL '16]



# Roadmap



**Multi-Band**

**The Future**

**Open Questions**

Frodo and Sam

BELEGAER  
(the Great Sea)



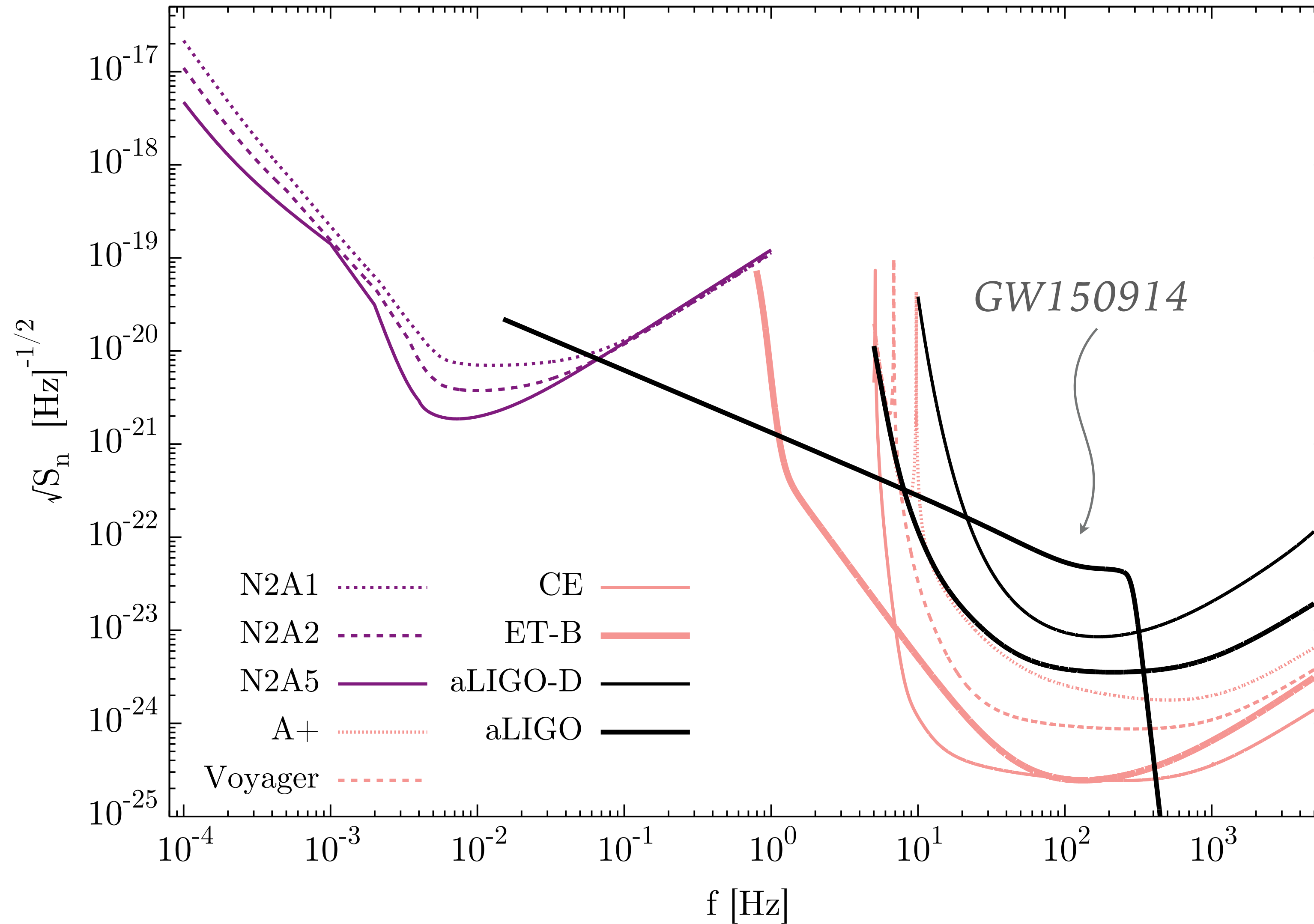
# Estúpidamente Preliminary



Greek for “somewhat”



# Spectral Noises of Future Instruments





In life you have to make choices, so we made some...

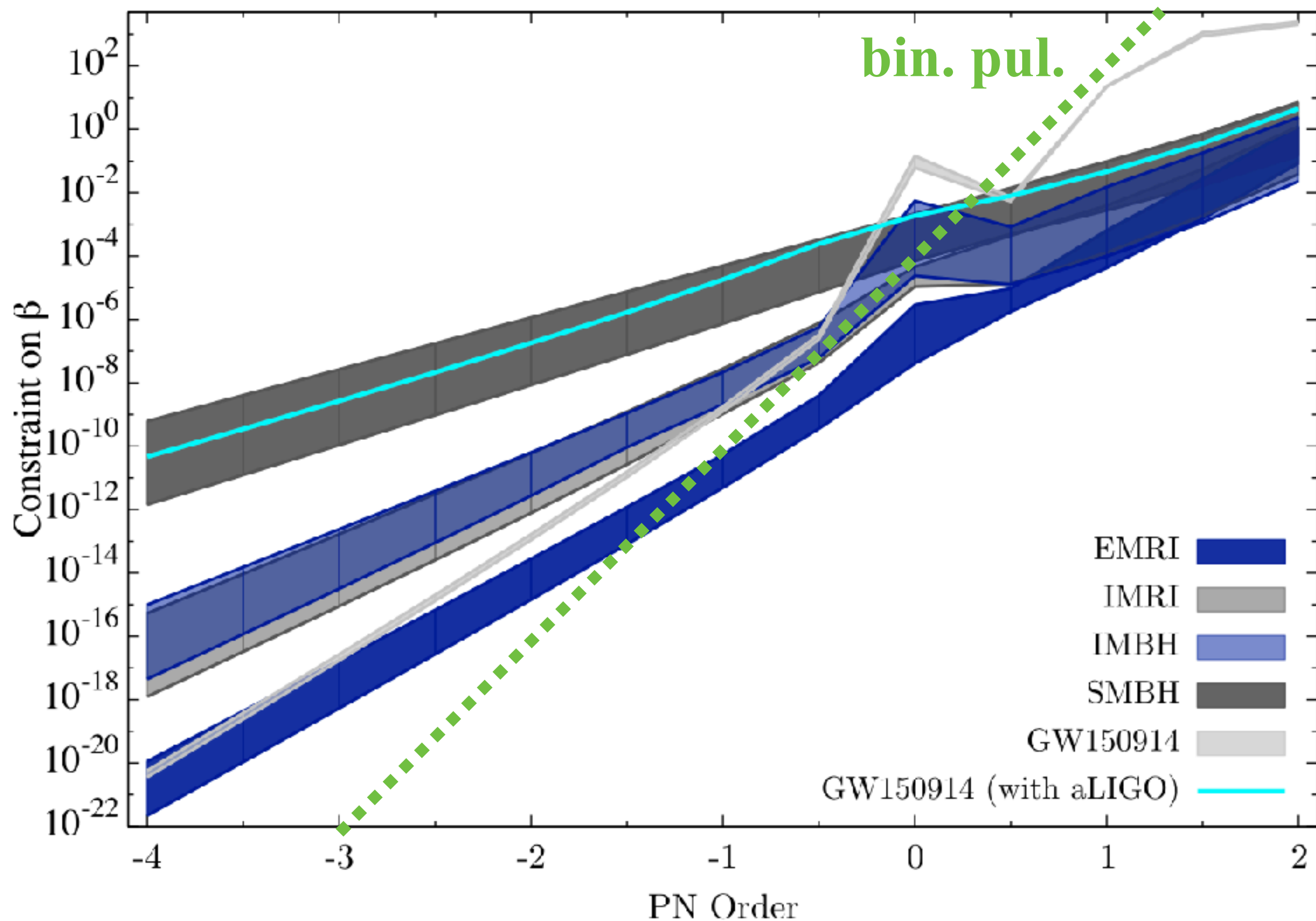
Name	$m_1 [M_\odot]$	$m_2 [M_\odot]$	$(\chi_1, \chi_2)$	$D_L$	$z$	$\rho$ -range
GW150914	35.1	29.5	(0.31, 0.39)	400 Mpc	$\sim 0.09$	6 – 12
EMRI	$10^5$	10	(0.8, 0.4)	1 Gpc	$\sim 0.2$	60 – 235
IMRI	$10^5$	$10^3$	(0.7, 0.9)	5 Gpc	$\sim 0.8$	166 – 659
IMBH	$5 \times 10^3$	$4 \times 10^3$	(0.7, 0.9)	16 Gpc	$\sim 2$	58 – 227
SMBH	$5 \times 10^6$	$4 \times 10^6$	(0.7, 0.9)	48 Gpc	$\sim 5$	372 – 1110

Name	$m_1 [M_\odot]$	$m_2 [M_\odot]$	$(\chi_1, \chi_2)$	$D_L$	$\rho_{aLIGO}$	$\rho_{A+}$	$\rho_{Voyager}$	$\rho_{ET-B}$	$\rho_{CE}$
NSNS	2	1.4	(0.01, 0.02)	100 Mpc	23.23	33.65	109.55	332.98	541.14
$\ell$ BHNS	5	1.4	(0.2, 0.02)	150 Mpc	22	31	103	312	511
$\ell$ BHBH	8	5	(0.2, 0.3)	250 Mpc	28	40	132	398	656
BHBH	25	20	(0.3, 0.4)	800 Mpc	26	38	123	372	615
GW150914	35.1	29.5	(0.31, 0.39)	400 Mpc	66	95	310	951	1556

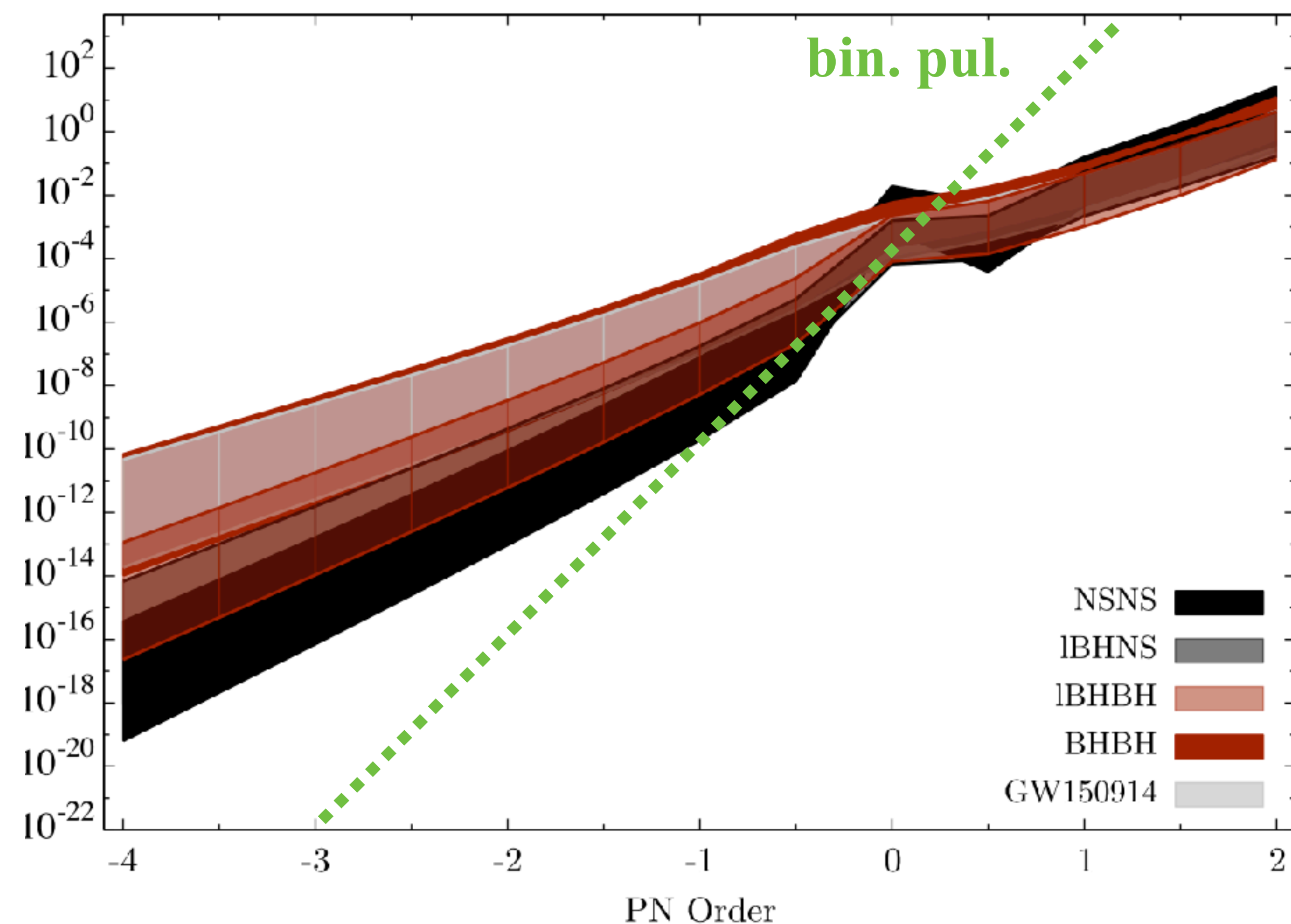


# Future ppE Constraints on GR

space-based



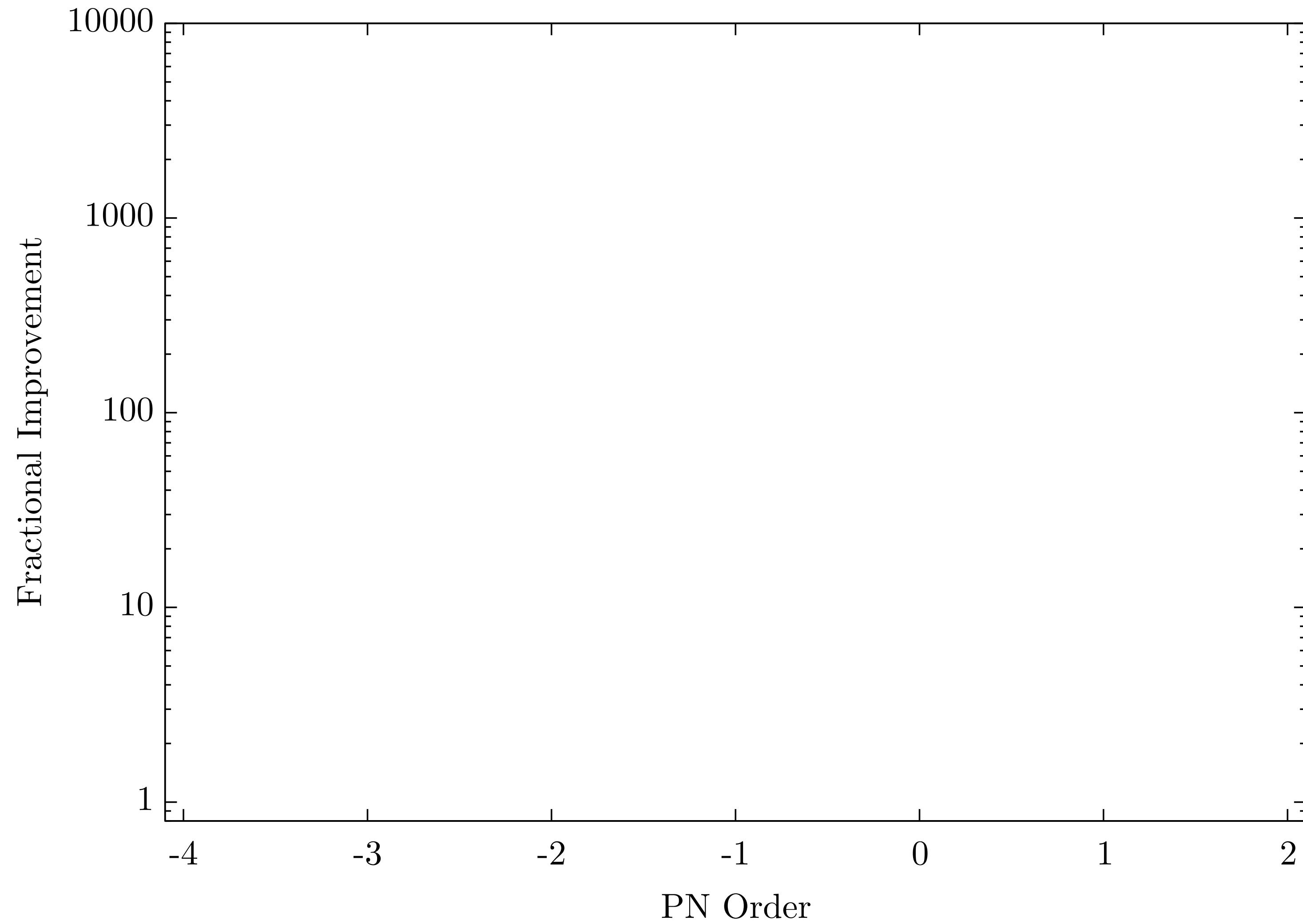
ground-based



[Chamberlain & Yunes, to appear soon]



# Fractional Improvement of ppE Constraints



[Chamberlain & Yunes, to appear soon]



# What are we really learning with GWs?

## Violations of the Strong Equivalence Principle

Lorentz Violations in Gravity

Gravitational Parity Violation

**What matters the most is the *mapping* between ppE constraints and theoretical physics inferences**

## Graviton Mass and Propagation Effects

- 
- 
- 

(leaving out a lot of stuff here, e.g. no-hair tests with ringdown)

# Future Constraints on the Graviton Mass

## Maximize Extraction:

Binary systems that are as far away as possible (SMBHs)

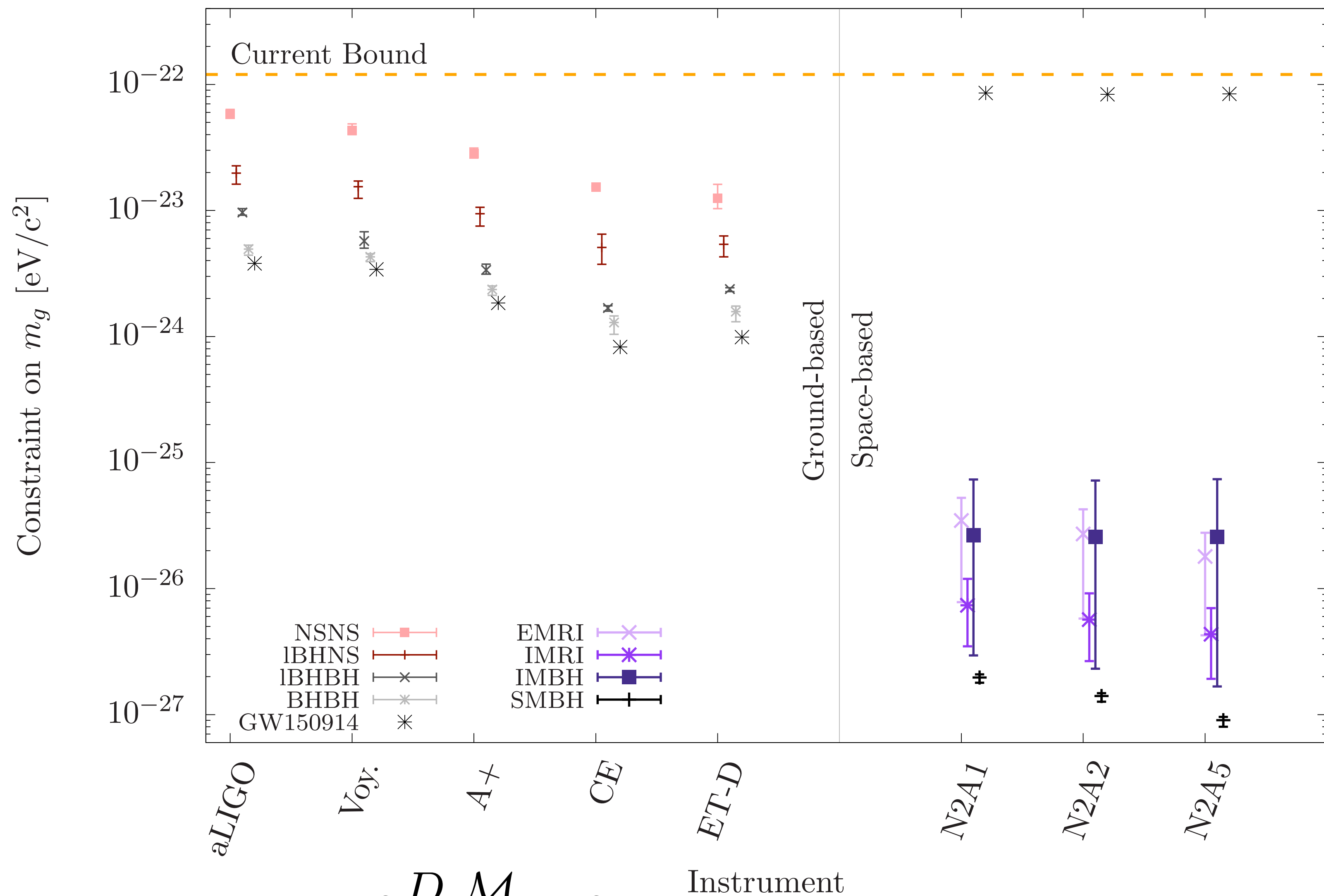
Binary with largest chirp mass

## Open Questions:

Generation of GWs?

Merger? Hybrid IMR waveforms?

**What is the Goal?**



$$\beta = \pi^2 \frac{D \mathcal{M}_z}{1+z} m_g^2$$

[Chamberlain & Yunes, to appear soon]



# Future Constraints on Violations of SEP

## Extractable Physics:

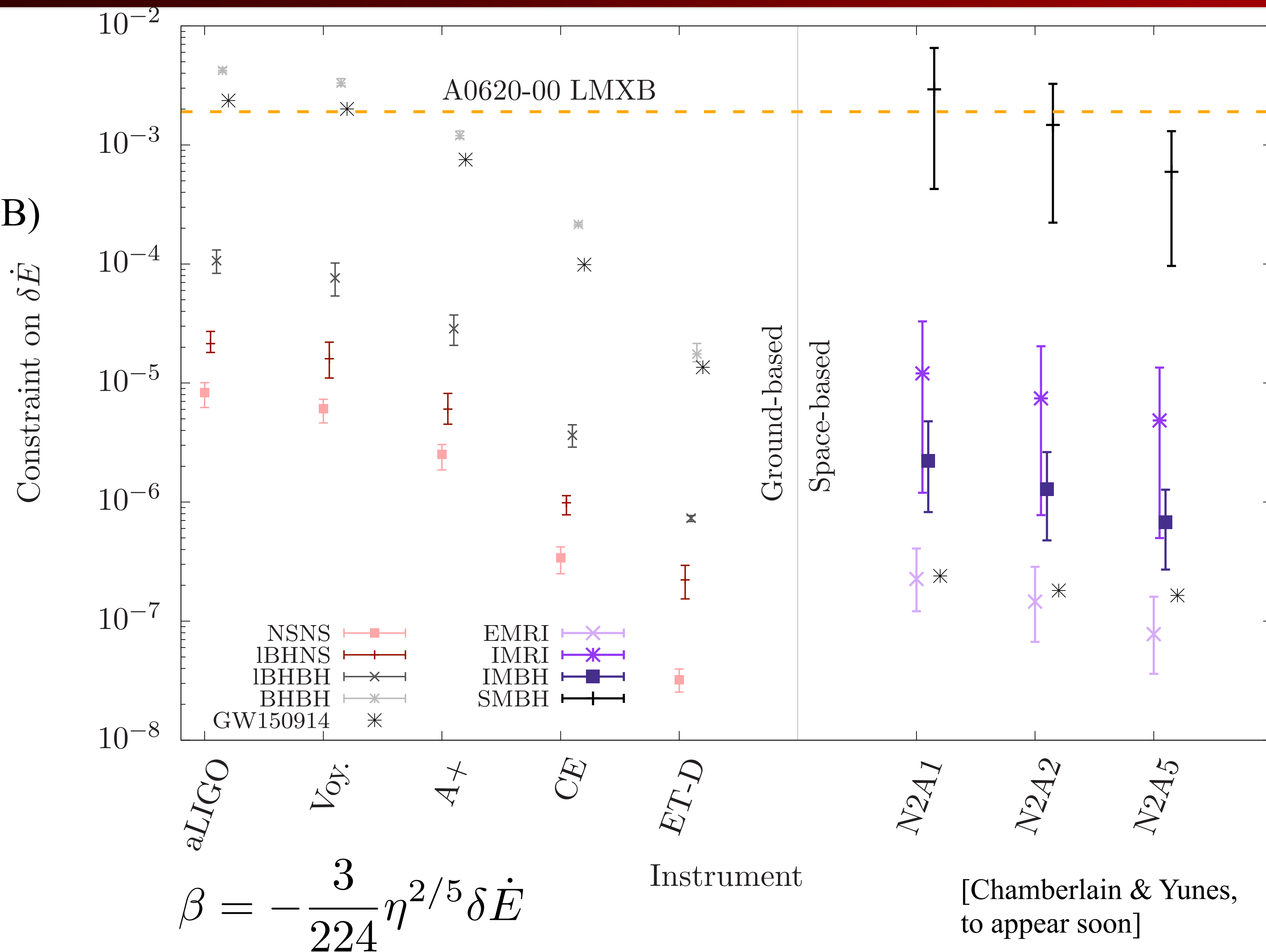
- Non-Schw BHs (yes-hair theorem in EdGB)
- NSs have scalar charge (scalar-tensor)
- Compact Object binaries inspiral faster due to dipole radiation

## Maximize Extraction:

- Low-mass BH or NS (long-inspiral) GWs
- Binary with tiny mass ratio

## Open Questions:

- Merger?
- Hybrid IMR waveforms?





# Future Constraints on Gravitational Lorentz Violation

## Extractable Physics:

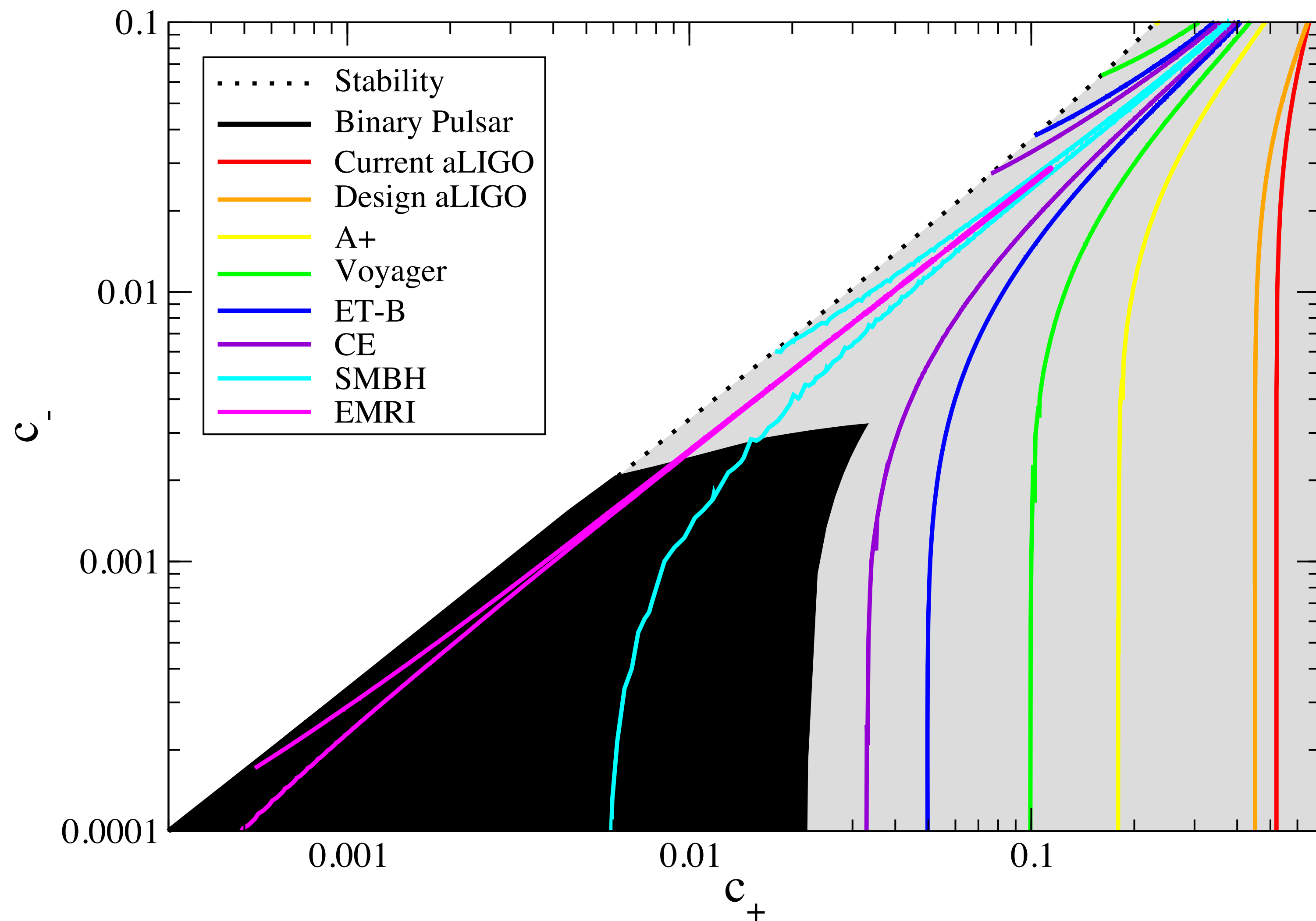
- Non-Spinning BH is not Schwarzschild
- NSs have sensitivity-dependent GR deviations
- Compact Object binaries inspiral faster (dipole

## Maximize Extraction:

- SMBHs or EMRIs do best

## Open Questions:

- BH sensitivities and Inspiral BH waveforms?
- Merger? Hybrid IMR waveforms?



$$\beta = \frac{3}{128} \text{nasty}(c_+, c_-)$$

[Chamberlain & Yunes, to appear soon]



# Future Constraints on the Variation of Newton's G

## Maximize Extraction:

Binary system at widest separation possible (lowest frequency)

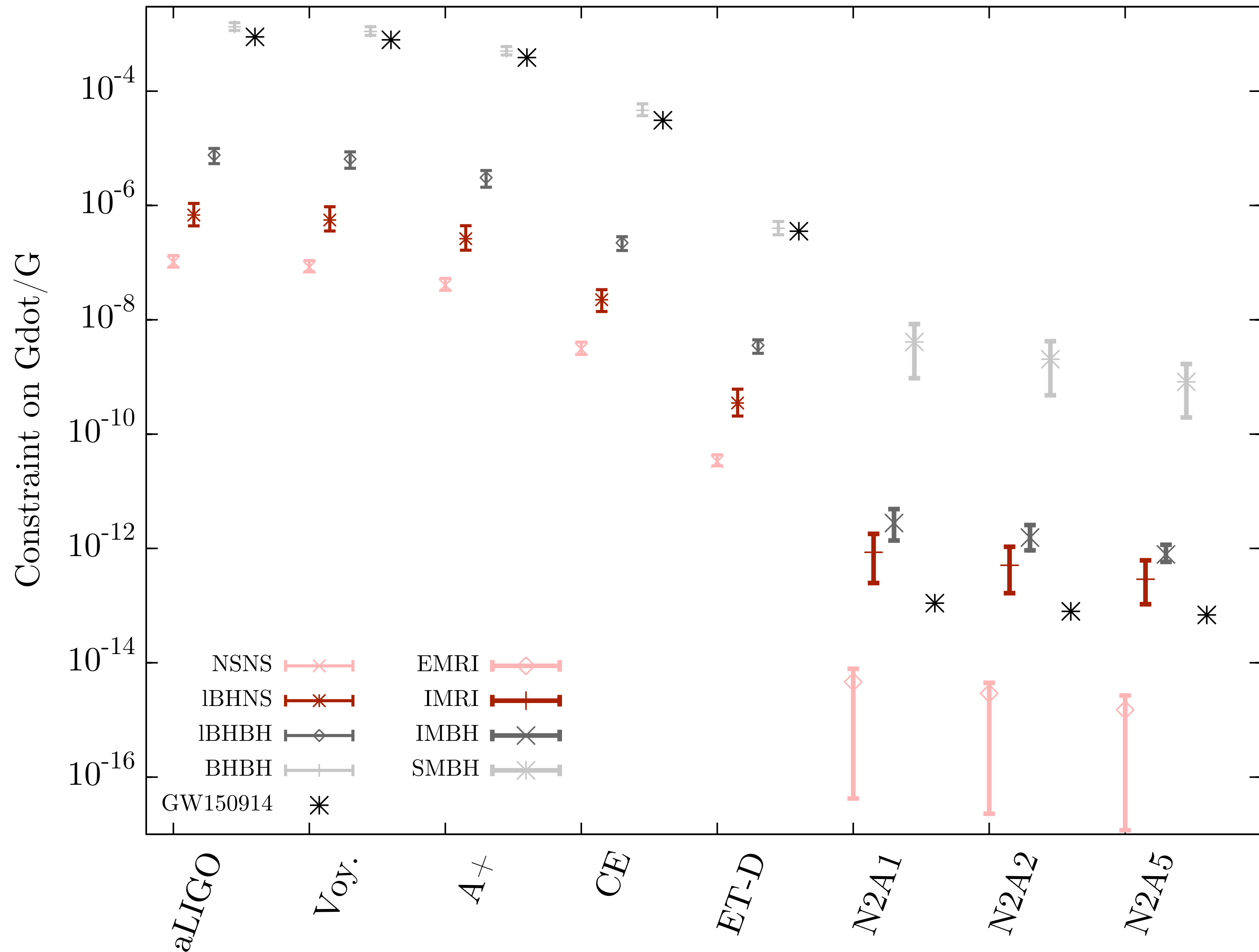
Binary with largest chirp mass

## Open Questions:

Generation of GWs?

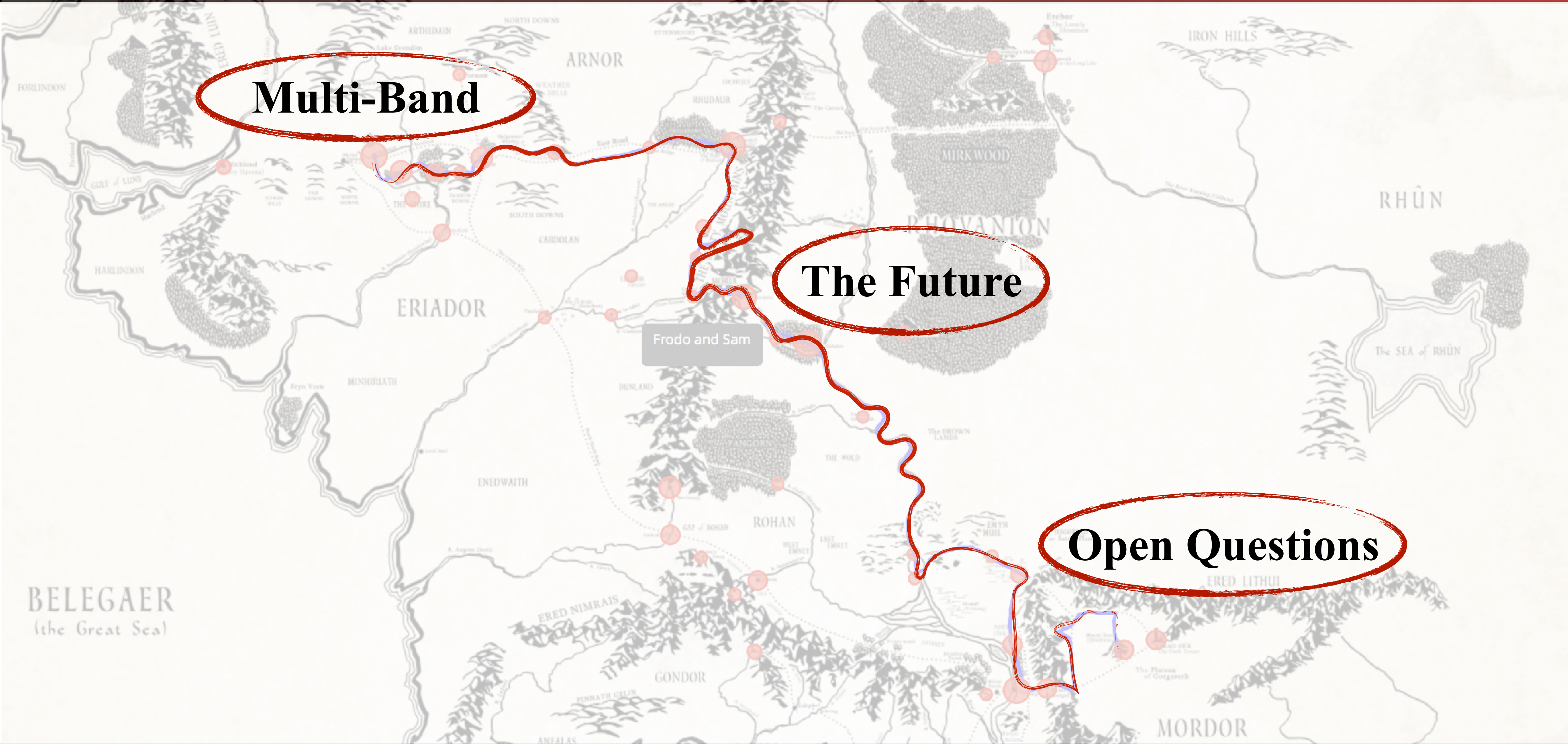
Merger? Hybrid IMR waveforms?

$$\beta = -\frac{25}{65526} \frac{\dot{G}}{G} \mathcal{M}_z \quad \text{[Chamberlain & Yunes, to appear soon]}$$





# Roadmap





# And now what?

**Why?**

**Duty**

**Curiosity**

**Religion**

**How?**

**More Consistency ?**

**Better ppE ?**

**Compelling Alternative?**



# Nico's Crystal Ball

**5 years**    Observations: 25/year

Detectors: aLIGO  $\rightarrow$  A+, AVirgo, Kagra

Theory: in GR: IMR of precessing inspirals and (maybe) eccentric  
in not GR: mergers and 1 PN in a few theories (e.g. EdGB)

---

**10 years**    Observations: 100/year

Detectors: A+  $\rightarrow$  Voyager, AVirgo, Kagra, Indian LIGO

Theory: in GR: single model for spin-precessing, eccentric, with NR calibration  
in not GR: mergers in more theories with spin precession

---

**15 years**    Observations: rate limited

Detectors: Voyager  $\rightarrow$  CE, aVirgo, aKagra, Indian LIGO, LISA

Theory: in GR: EMRIs (with second-order self-force)  
in not GR: EMRIs in modified gravity?

# Some Open Problems

## Theory

New & Interesting Physical Mechanisms?

Cosmological Modified Theories?

Spin Precession in Modified Gravity?

Mergers in Modified Gravity?

EMRIs and resonances in Modified Gravity?

“New” sources of GWs? (eg. eccentric)

## Experiment

Efficient data analysis w/spin precession?

Reduced Order Methods for Mod. Grav. ?

Improved instruments vs new instruments?

Combining EM information ?

Ringdown tests? Stacking?



**Thank You**

# Future Constraints on Gravitational Parity Violation

Left/Right polarized waves propagate differently

$$\beta_{\text{acs}} = \frac{1549225}{11812864} \frac{\zeta_{\text{dcs}}}{\eta^{14/5}} \left[ \left( 1 - \frac{231808}{61969} \eta \right) \chi_s^2 + \left( 1 - \frac{16068}{61969} \eta \right) \chi_a^2 - 2\delta_{mn} \chi_s \chi_a \right],$$

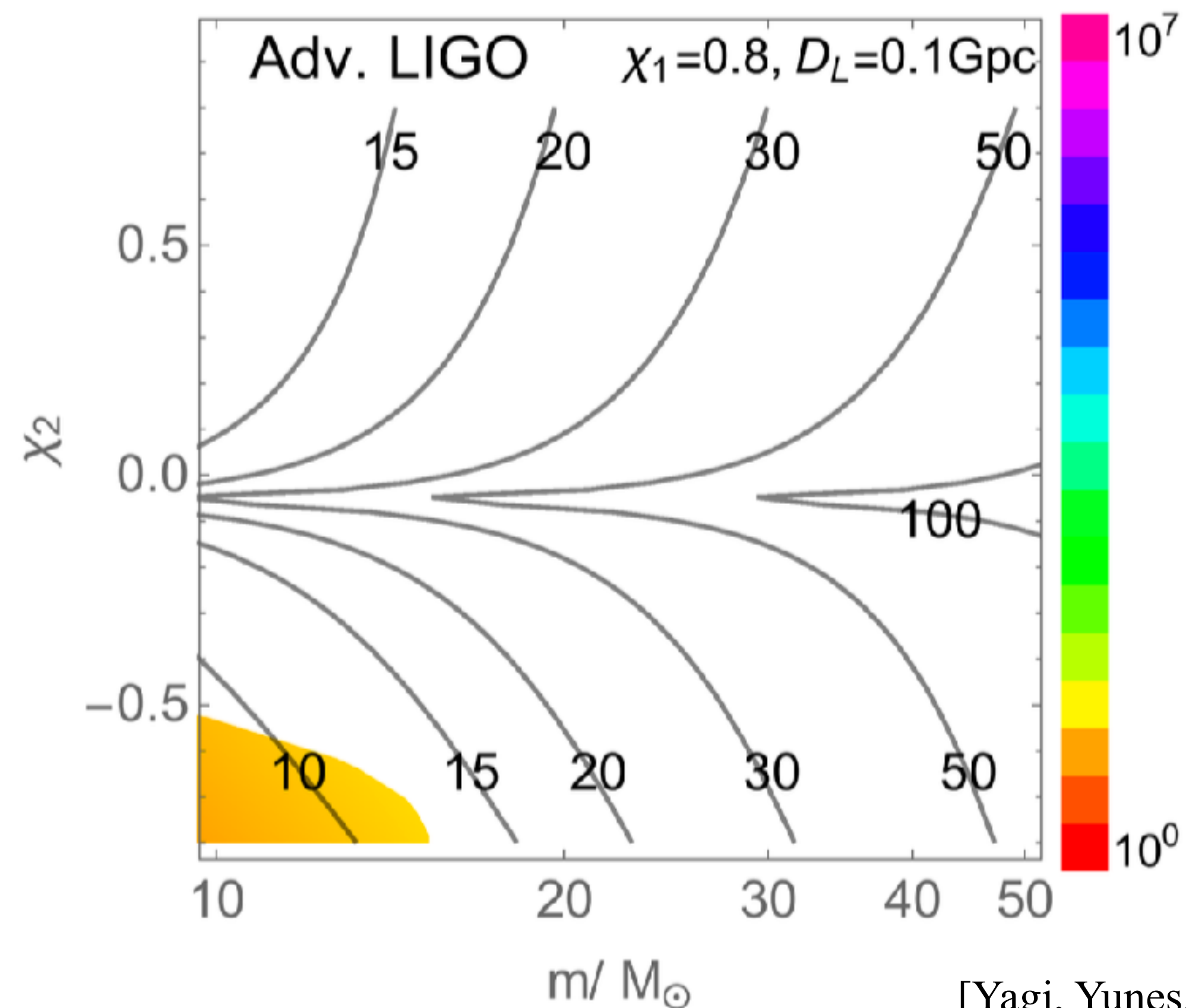
**Extractable Physics:** Spinning BH is not Kerr (yes-hair theorem)

Spinning BH binaries inspiral faster (magnetic dipole)

**Maximize Extraction:**

Low-mass (long-inspiral)  
high spin (precession)  
BH binaries

**Open Questions:** Merger? Hybrid IMR waveforms?



[Yagi, Yunes, Tanaka, PRL '13]



# Parametrized post-Einsteinian Framework

## The parameterized post-Einsteinian Framework

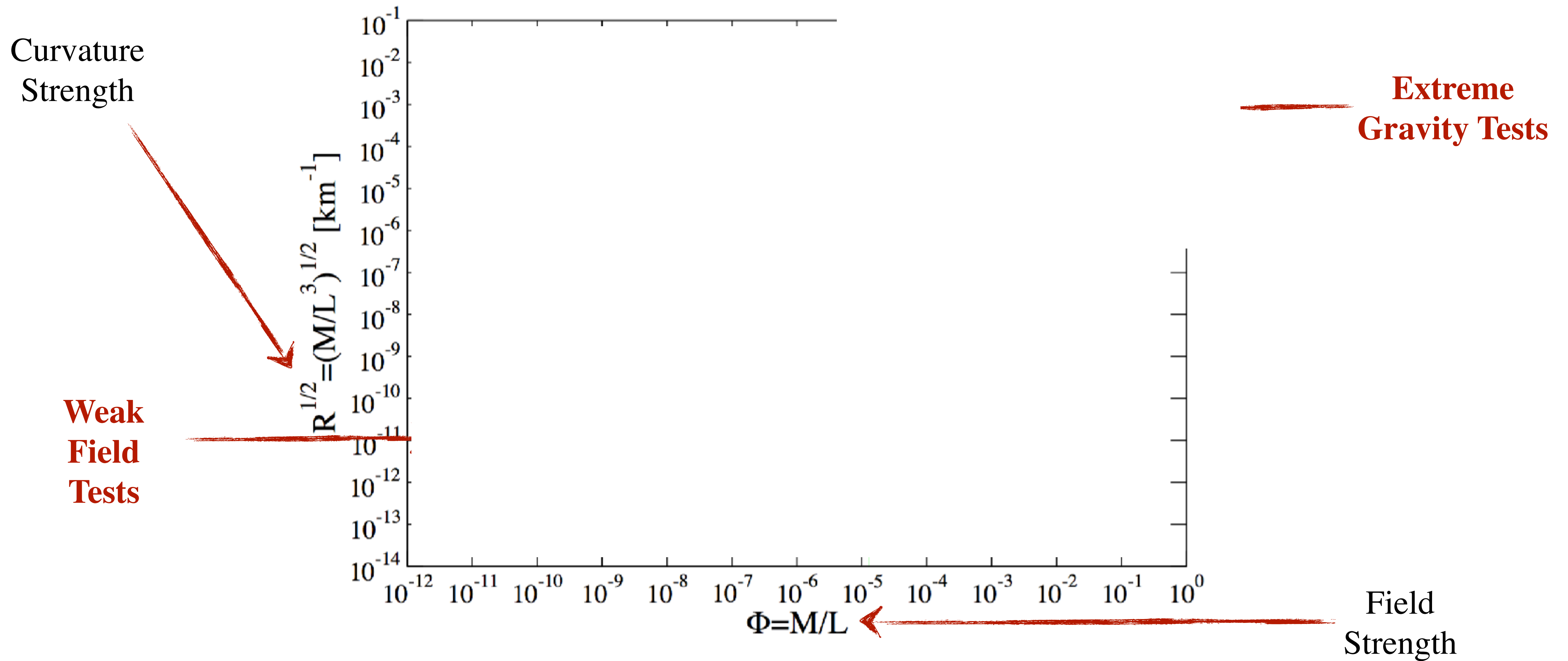
$$\tilde{h}(f) = \tilde{h}_{GR}(f) (1 + \alpha f^a) e^{i\beta f^b}$$

[Yunes & Pretorius,  
PRD 2009]

Theoretical Effect	Theoretical Mechanism	Theories	ppE $b$	Order	Mapping
Scalar Dipolar Radiation	Scalar Monopole Field Activation BH Hair Growth	EdGB [140, 142, 149, 150]	-7	-1PN	$\beta_{\text{EdGB}}$ [140]
		Scalar-Tensor Theories [59, 151]	-7	-1PN	$\beta_{\text{ST}}$ [59, 151]
Anomalous Acceleration	Extra Dimension Mass Leakage Time-Variation of $G$	RS-II Braneworld [152, 153]	-13	-4PN	$\beta_{\text{ED}}$ [141]
		Phenomenological [137, 154]	-13	-4PN	$\beta_{\dot{G}}$ [137]
Scalar Quadrupolar Radiation Scalar Dipole Force Quadrupole Moment Deformation	Scalar Dipole Field Activation due to Gravitational Parity Violation	dCS [140, 155]	-1	+2PN	$\beta_{\text{dCS}}$ [146]
Scalar/Vector Dipolar Radiation Modified Quadrupolar Radiation	Vector Field Activation due to Lorentz Violation	EA [109, 110], Khronometric [111, 112]	-7	-1PN	$\beta_{\text{E}}^{(-1)}$ [113]
			-5	0PN	$\beta_{\text{E}}^{(0)}$ [113]
Modified Dispersion Relation	GW Propagation/Kinematics	Massive Gravity [156–159]	-3	+1PN	$\beta_{\text{MDR}}$ [145, 156]
		Double Special Relativity [160–163]	+6	+5.5PN	
		Extra Dim. [164], Horava-Lifshitz [165–167],	+9	+7PN	
		gravitational SME ( $d = 4$ ) [179]	+3	+4PN	
		gravitational SME ( $d = 5$ ) [179]	+6	+5.5PN	
		gravitational SME ( $d = 6$ ) [179]	+9	+7PN	
Multifractional Spacetime [168–170]	3–6	4–5.5PN			

[MSU: Cornish et al PRD 84 ('11), Sampson et al PRD 87 ('13), Sampson, et al PRD 88 ('13), Sampson et al PRD 89 ('14),  
Nikhef: Del Pozzo et al PRD 83 ('11), Li et al PRD 85 ('12), Agathos et al PRD 89 ('14), Del Pozzo et al CQG ('14).]

# Strong Gravity versus Extreme Gravity

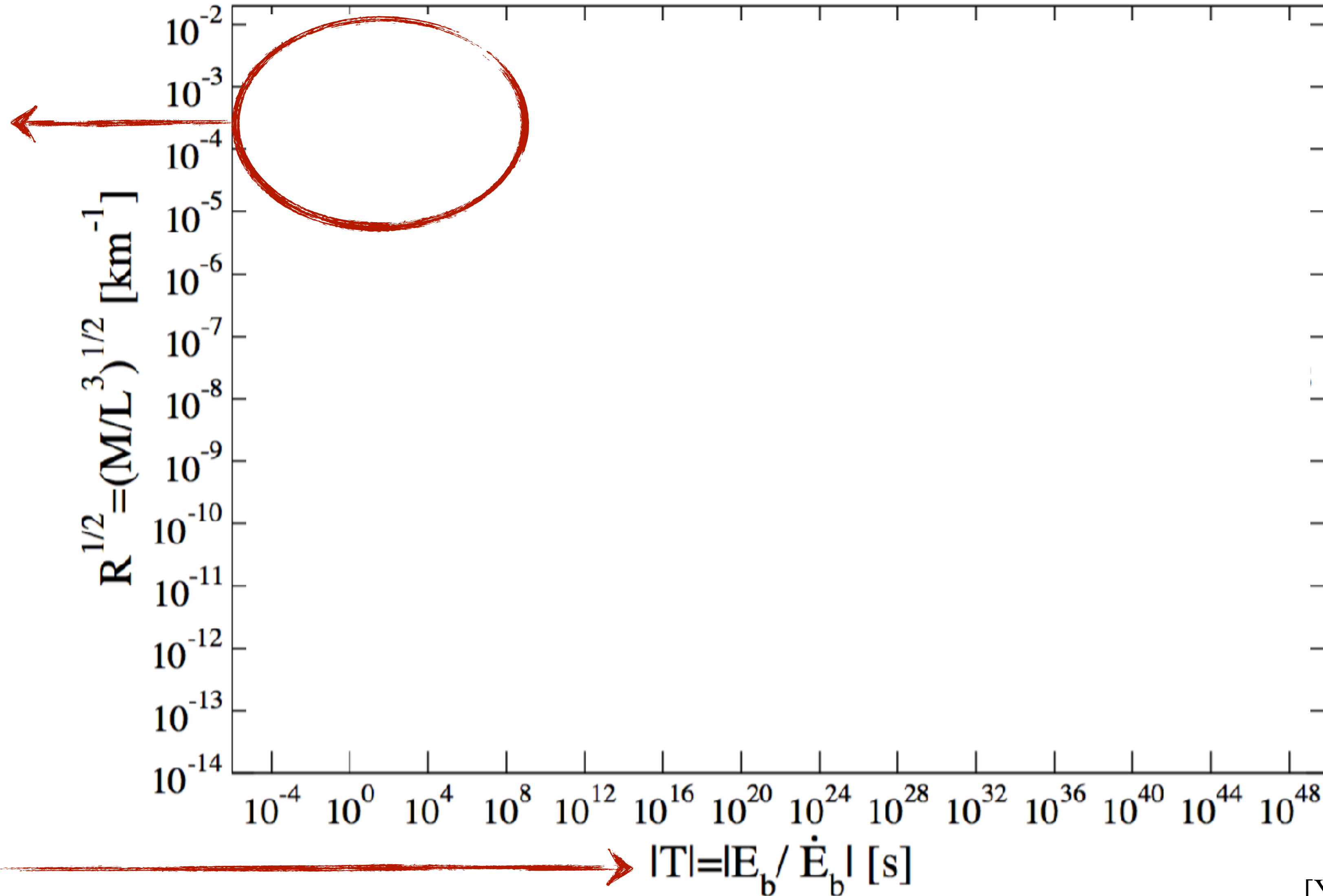


[Will, Liv. Rev., 2005, Psaltis, Liv. Rev., 2008, Baker, et al, Siemens & Yunes, Liv. Rev. 2013, Yunes, et al PRD 2016]



# Extreme Gravity versus Strong Gravity

Extreme Gravity Tests

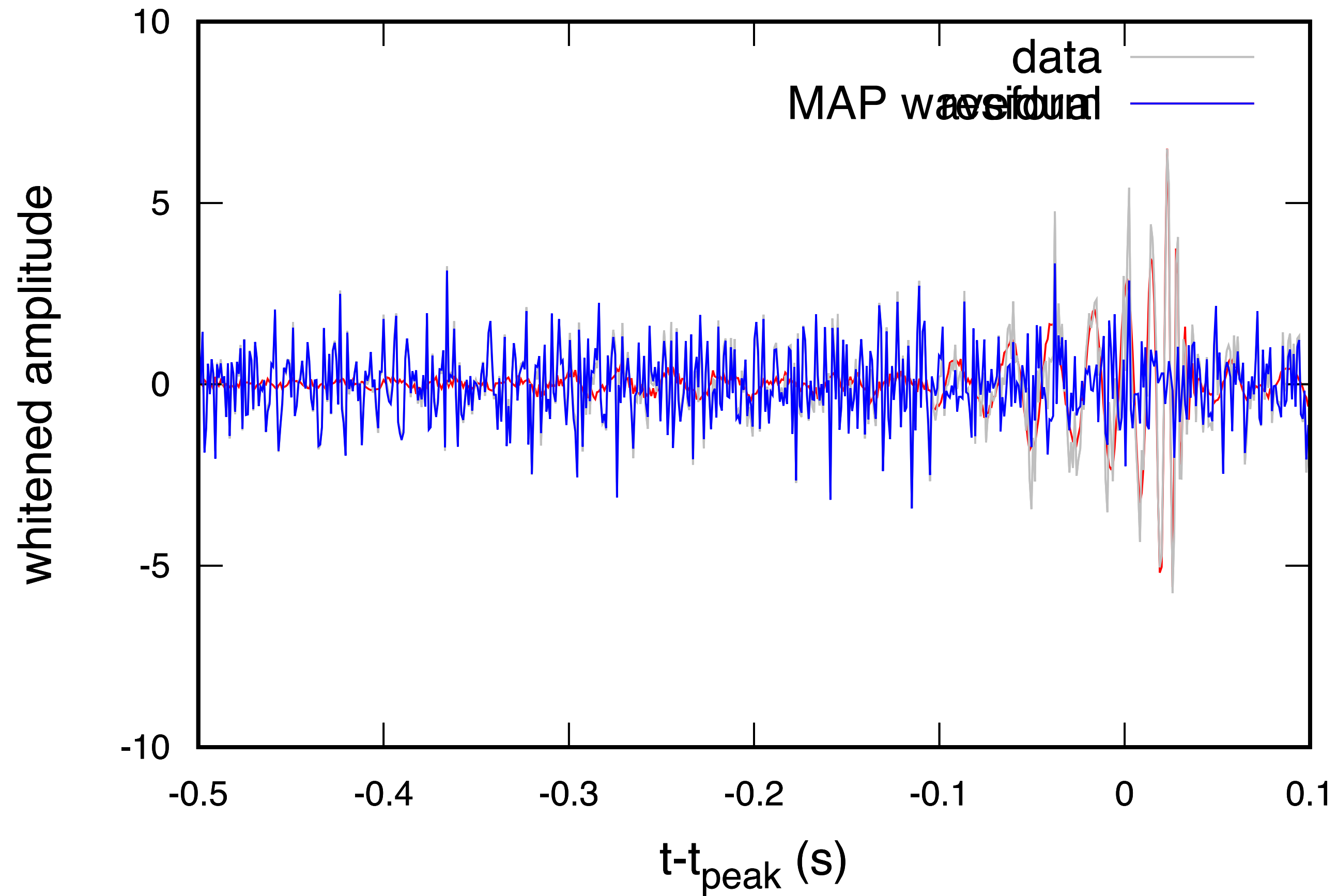


Dynamical Timescale

[Yunes, Yagi, Pretorius, PRD '16]

# Residual Consistency

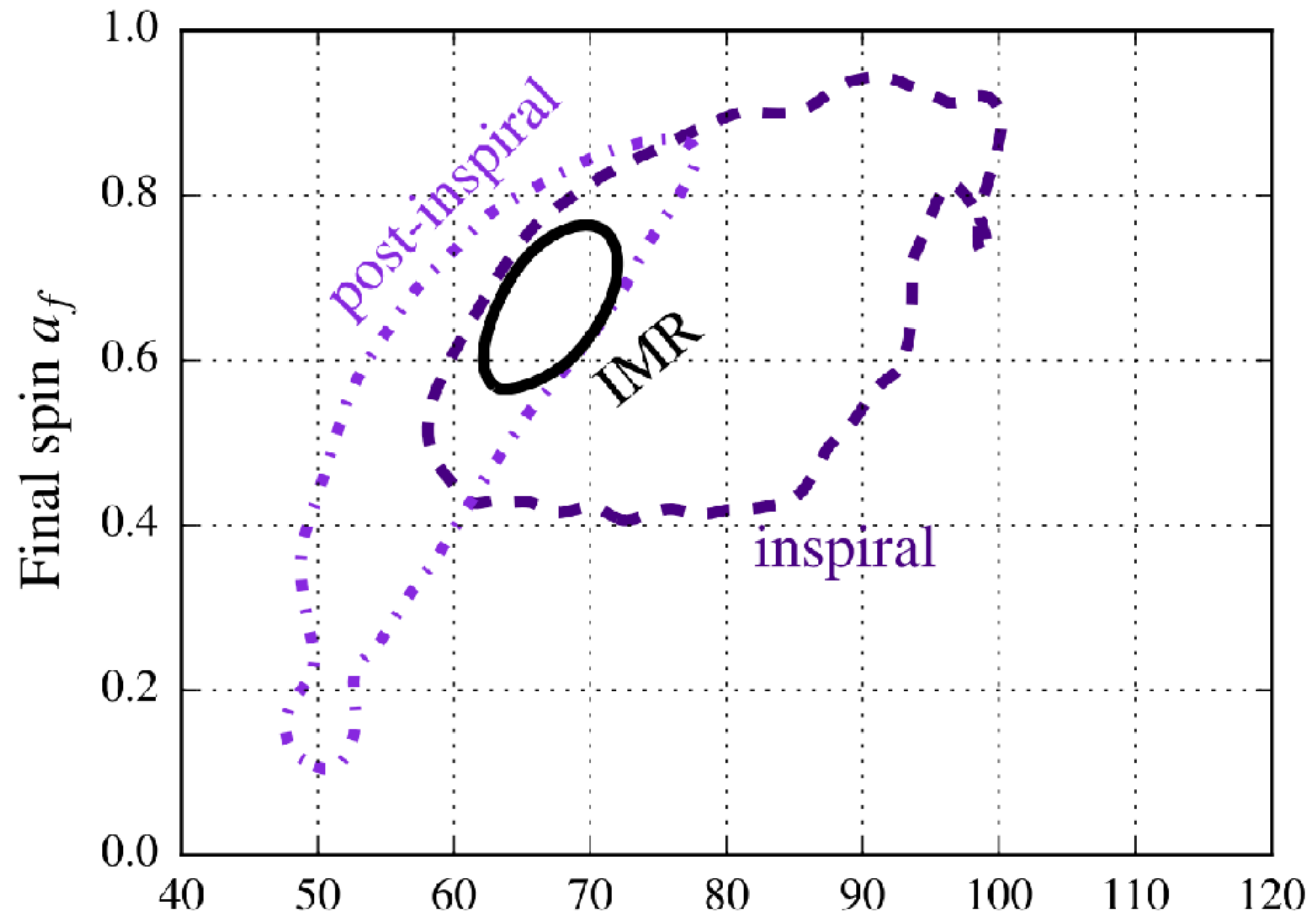
[Littenberg & Cornish]



**SNR of Residual (data - best fit) is consistent with noise**



# (Sort of) Jack-knife Consistency



# Classifying Deviations

## Gravitational Wave Generation

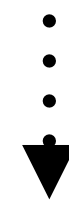
Scalar/Vector Field Activation

Gravitational Parity Violation

Gravitational Lorentz Violation

Extra-Dimensional Leakage

Time-Variation of  $G$



Spacetime Dimensionality

Parity Violation

Lorentz Violation

SEP Violation

## Gravitational Wave Propagation

Modified Dispersion Relations

Modified Kinematics

Gravitational Lorentz Violation

Cosmological Screening

Time-Variation of  $G$



Speed of Gravity

Mass of Graviton

Lorentz Violation

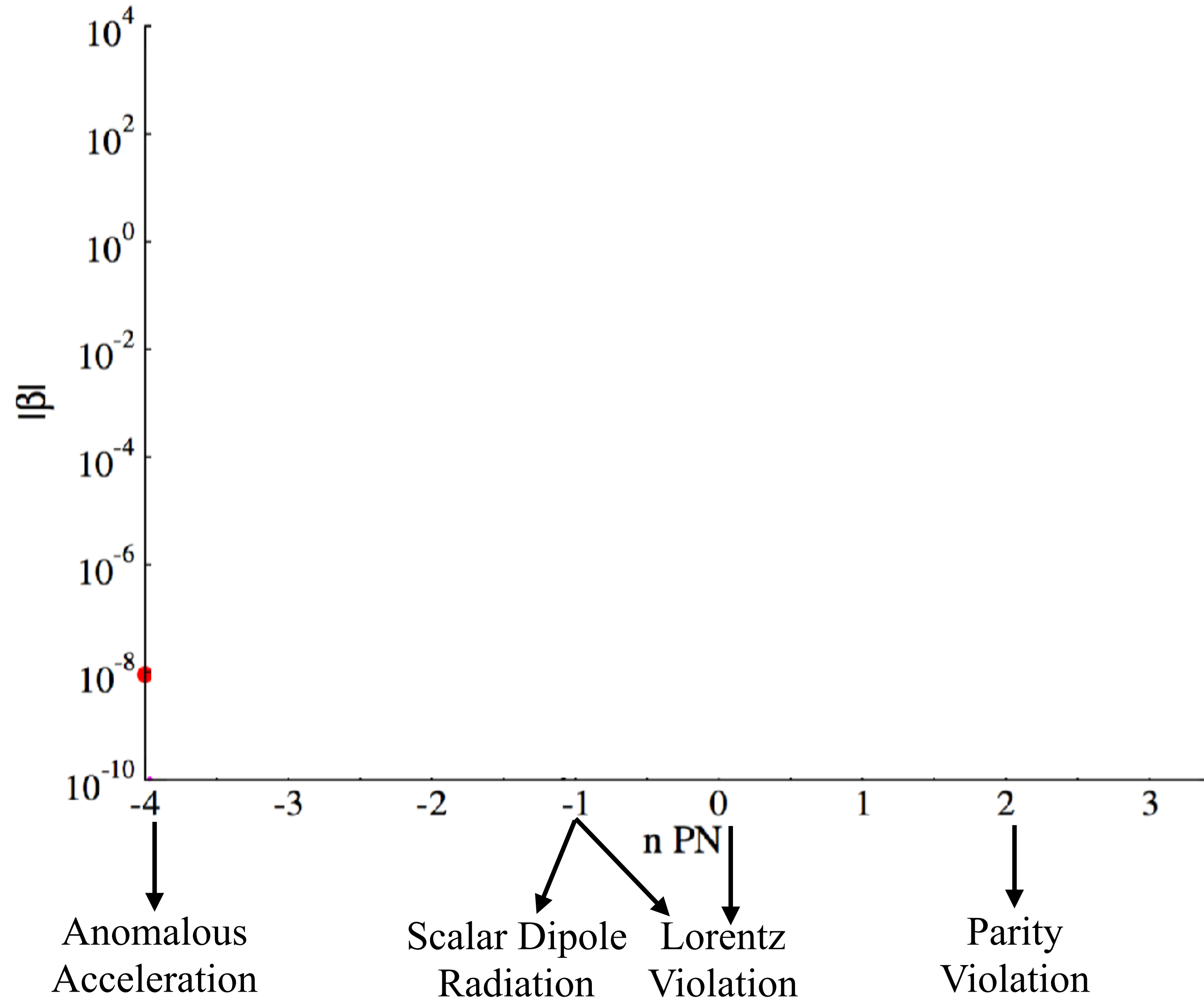
SEP Violation

**Test  
Fundamental  
Pillars  
of GR**



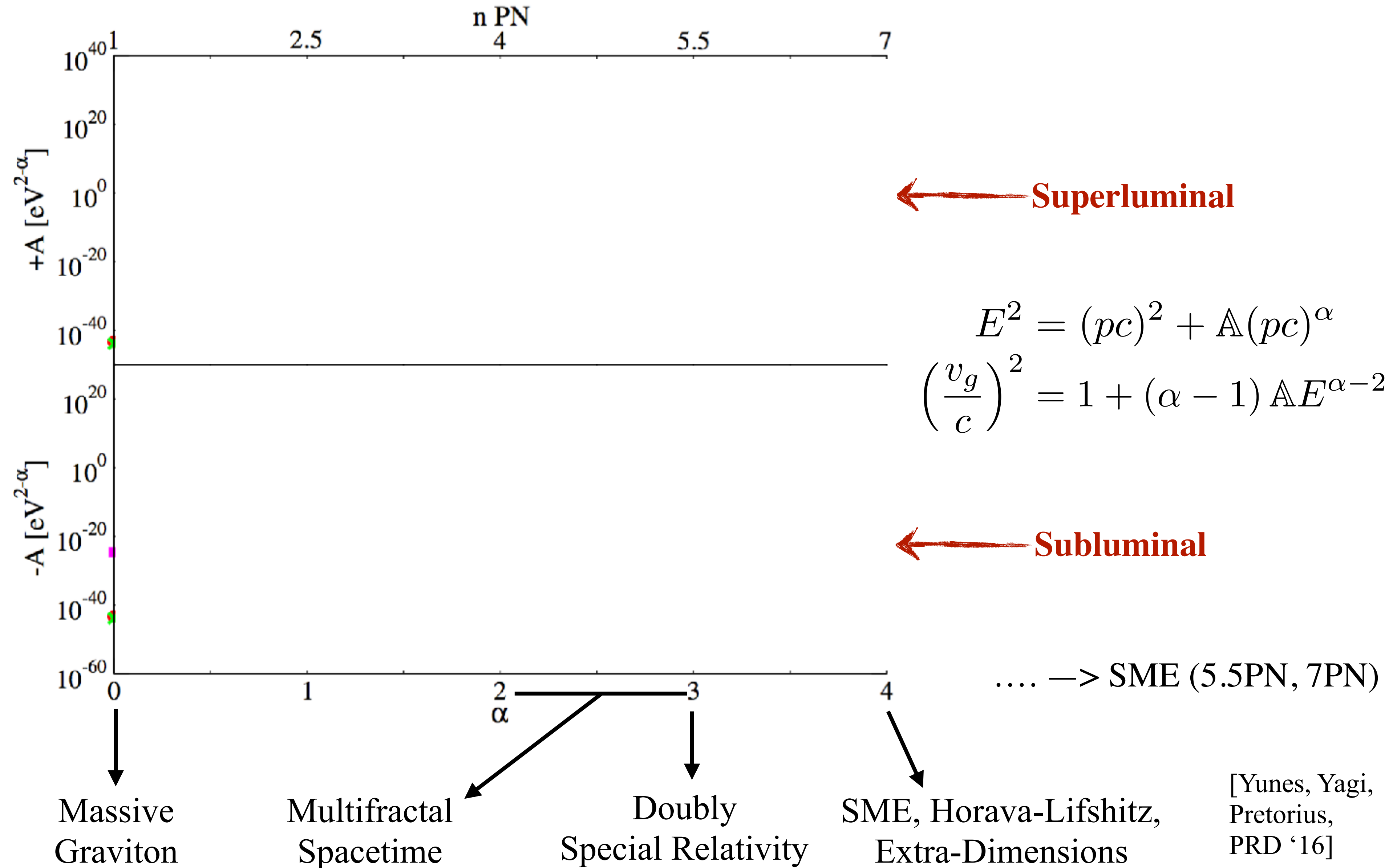


# O1 Constraints on GW Generation Effects



[Yunes, Yagi,  
Pretorius,  
PRD '16]

# O1 Constraints on Propagation Effects





# Theoretical Physics Implications

Theoretical Mechanism	GR Pillar	PN	$ \beta $		Repr. Parameters	Example Theory Constraints		
			GW150914	GW151226		GW150914	GW151226	Current Bounds
Scalar Field Activation	SEP	-1	$1.6 \times 10^{-4}$	$4.4 \times 10^{-5}$	$\sqrt{ \alpha_{EdGB} }$ [km] $ \dot{\phi} $ [1/sec]	—	—	$10^7$ [56], 2 [57–59] $10^{-6}$ [60]
Scalar Field Activation	SEP, PI	+2	$1.3 \times 10^1$	4.1	$\sqrt{ \alpha_{dCS} }$ [km]	—	—	$10^8$ [61, 62]
Vector Field Activation	SEP, LI	0	$7.2 \times 10^{-3}$	$3.4 \times 10^{-3}$	$(c_+, c_-)$ $(\beta_{KG}, \lambda_{KG})$	(0.9, 2.1) (0.42, —)	(0.8, 1.1) (0.40, —)	(0.03, 0.003) [63, 64] (0.005, 0.1) [63, 64]
Extra Dimensions	4D	-4	$9.1 \times 10^{-9}$	$9.1 \times 10^{-11}$	$\ell$ [ $\mu\text{m}$ ]	$5.4 \times 10^{10}$	$2.0 \times 10^9$	$10\text{--}10^3$ [65–69]
Time-Varying $G$	SEP	-4	$9.1 \times 10^{-9}$	$9.1 \times 10^{-11}$	$ \dot{G} $ [ $10^{-12}/\text{yr}$ ]	$5.4 \times 10^{18}$	$1.7 \times 10^{17}$	0.1–1 [70–74]

[Yunes, Yagi, Pretorius, PRD ‘16]